

Physics-based Compact Models for Biosensors, Landau Transistors, & Thin-Film Solar Cells

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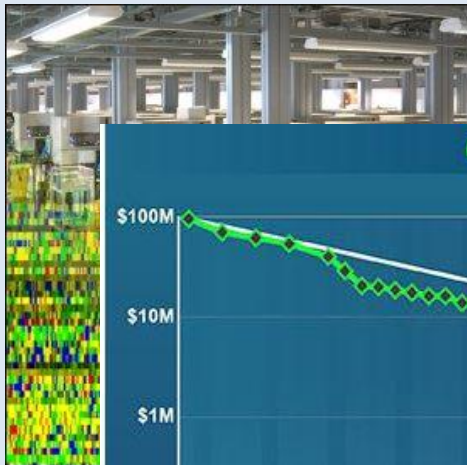
<http://nanohub.org/resources/16560>
cobweb.ecn.purdue.edu/~alam

Outline

- Is there a life after Moore's Law?
- Power sources: Harvesters, solar cells, etc.
- Implantable and clinical nanobiosensors
- Low-power Landau switches
- The challenges of integrated simulation
- Conclusions

Life after Moore's law: The Transistor is Dead, Long live The Transistor

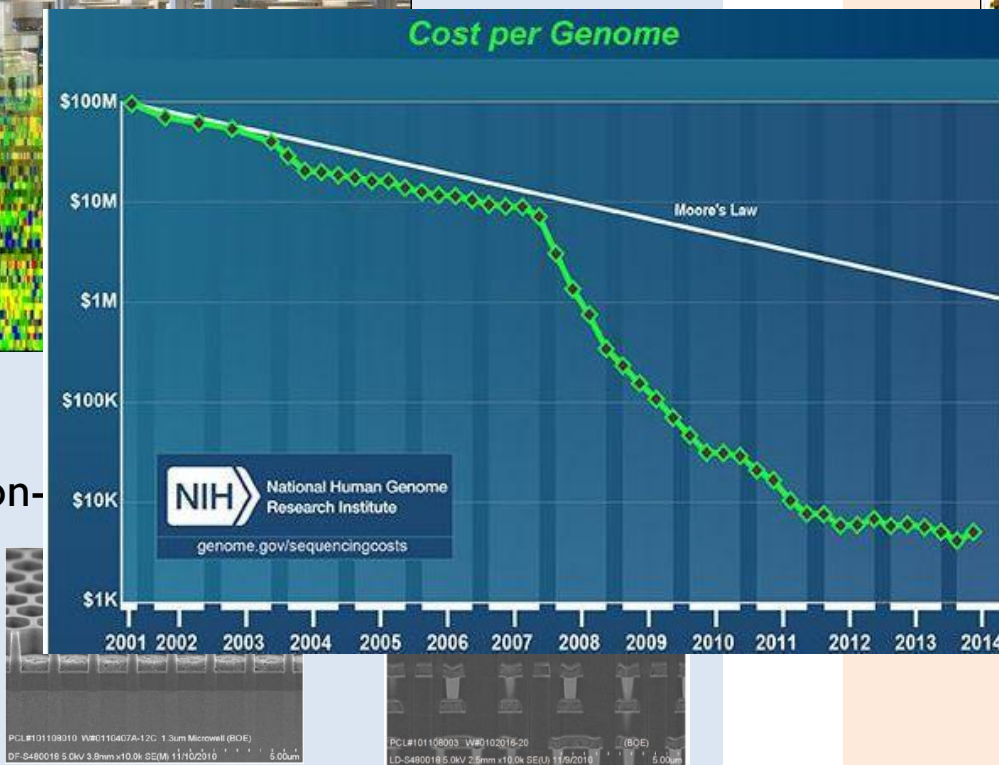
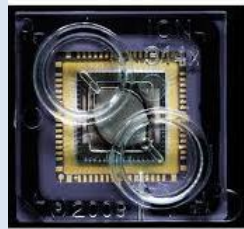
Sanger method (1990s)



Babbage computer (~1830s)



Ion-



Intel Chip Today



Live After Moore's law: End-to-end modeling of solar cells



Scaling up can
induce efficiency gap



Record cell efficiency >22%

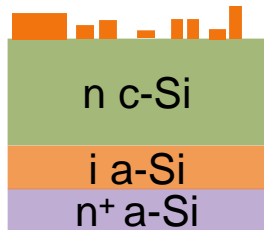
State-of-the-art commercial panels: 19.4%

Process variations

Contacts and shunts

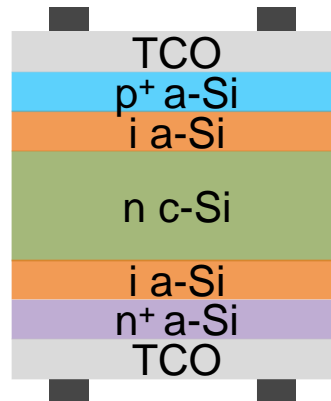
Grid resistance, shading etc.

Process
parameters



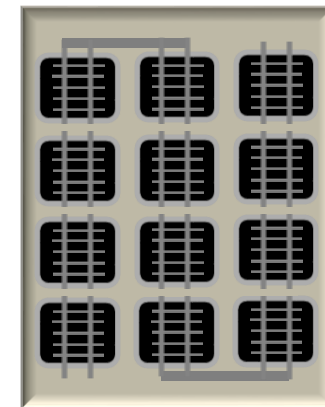
Process stage

a-Si film
properties



Device stage

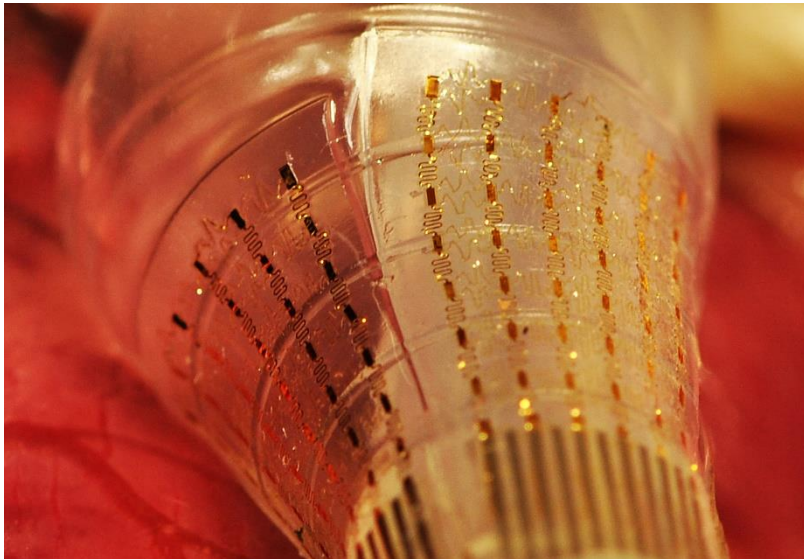
Cell
 $I - V$



Panel stage

Panel η

Life after Moore's Law: Heterogeneous integration on active substrate

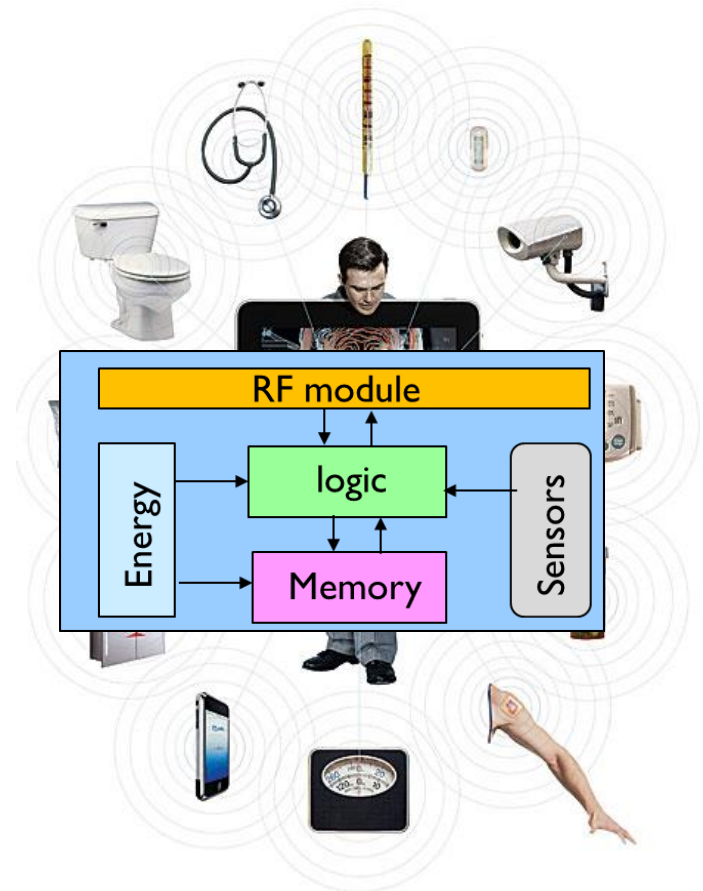


Reliability in fluids
Energy harvesting
Noise immunity
Biofouling

M.A.Alam, Purdue University, 2015

Life after Moore's Law: Internet of (too many?) things ...

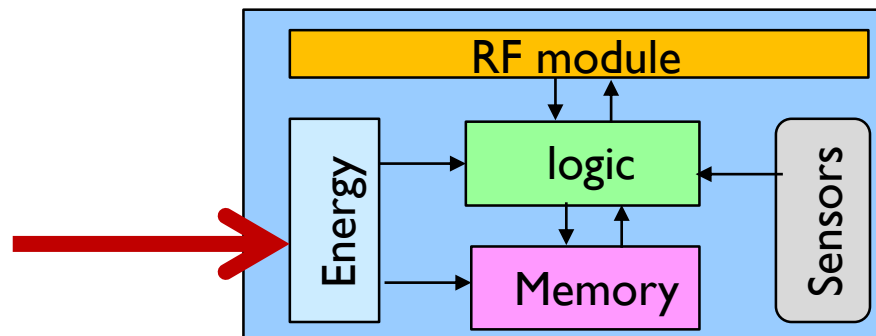
Lab-on-a-phone
(nano+biotechnology)



Always on sensor network
(nanotechnology + biotechnology + wireless technology)

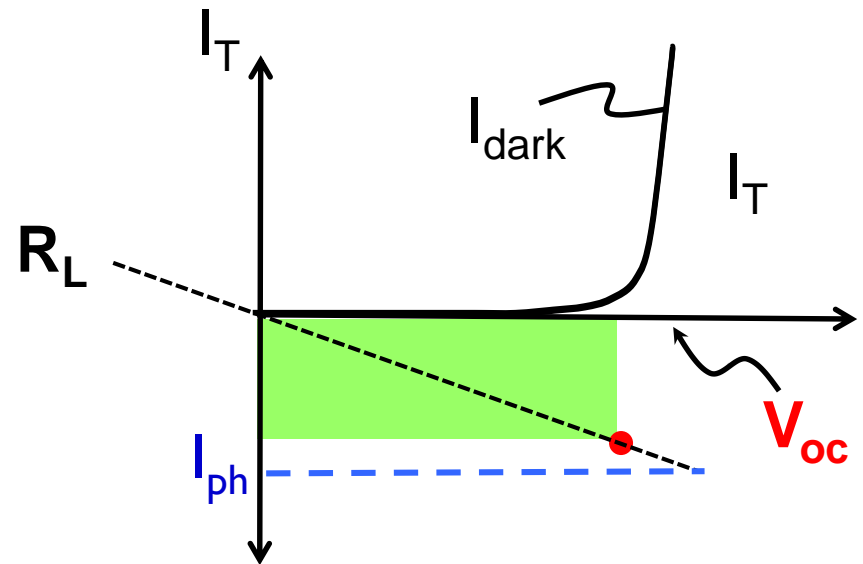
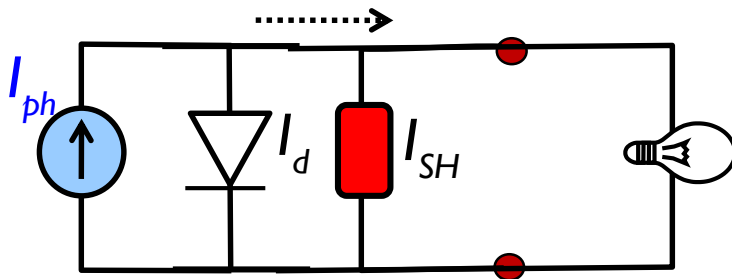
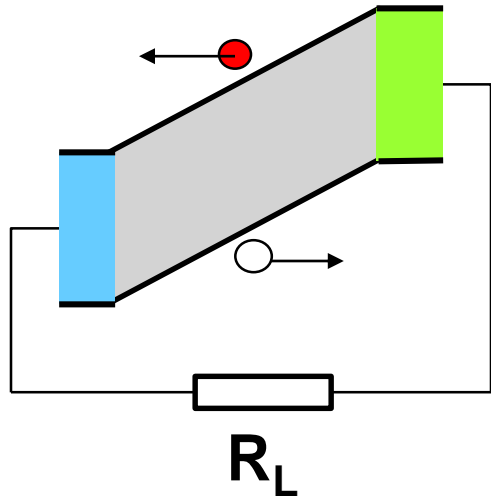
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Basics of solar cell operation

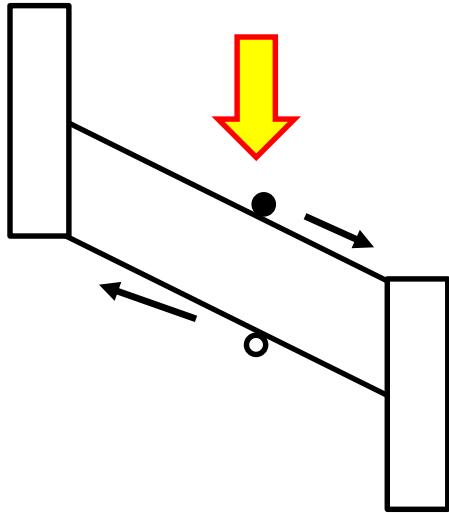
Alam, Proc. IRPS, p. 312, 2010.



Voltage independent photocurrent
Good for c-Si, but almost nothing else

Technology-agnostic end-to-end modeling

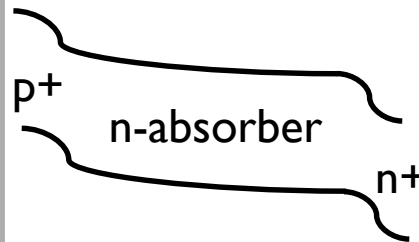
Ideal solar cell



- Photo-generation in absorber layer only
- Strong electric field to push carriers to contacts
- Carrier selective contacts to minimize recombination

Reality

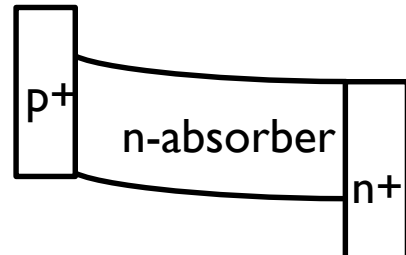
p-n homojunction



p-i-n homojunction

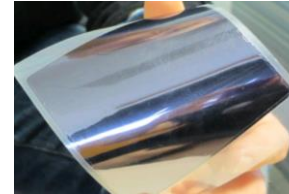


P-n heterojunction



Technologies

High Performance & High Costs



GaAs



c-Si

Low Performance & Low Costs

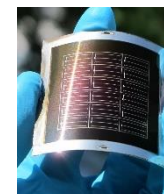


a-Si cell

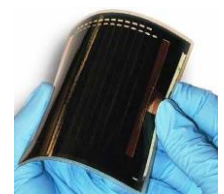
High Performance & Low Costs



HIT cell

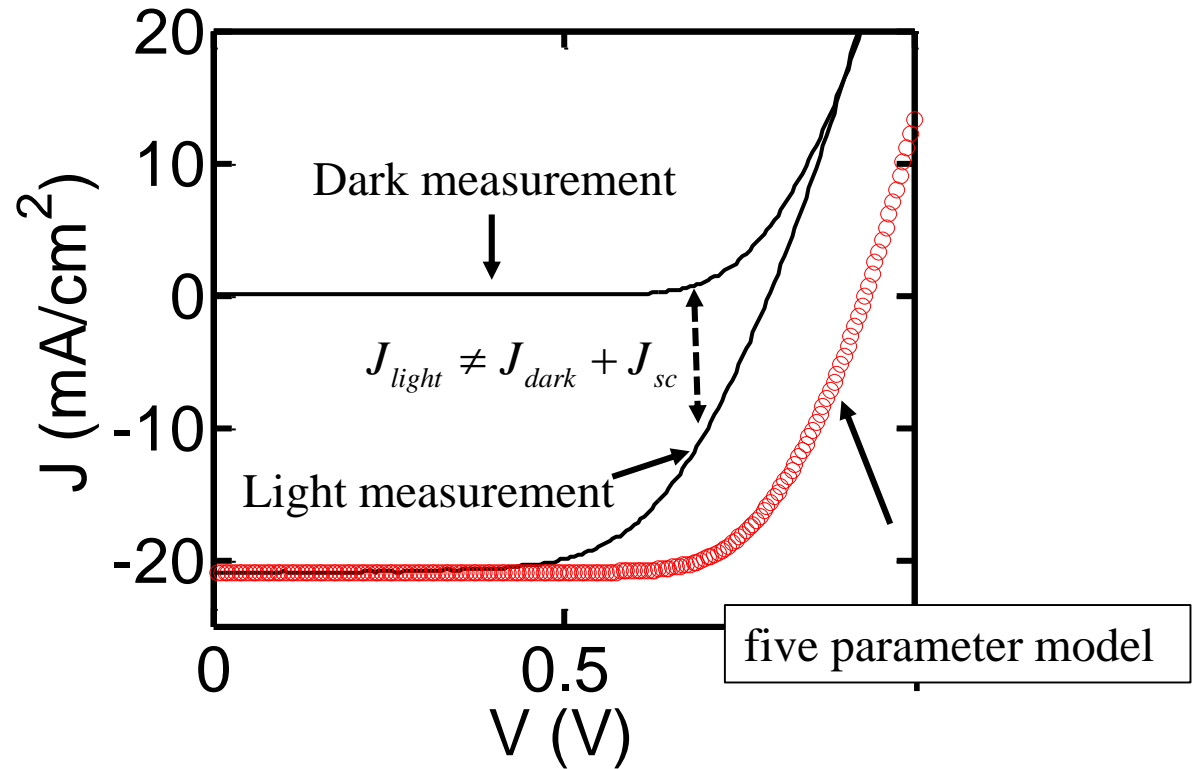
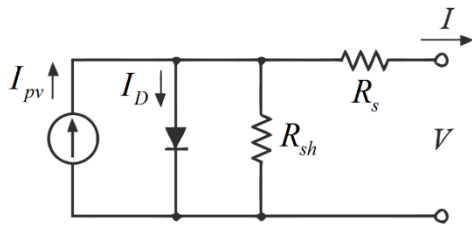


CdTe



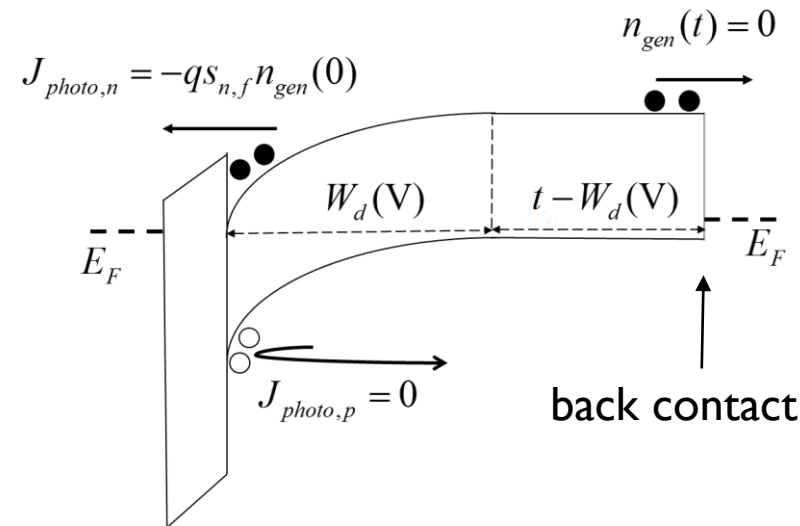
CIGS

Si Compact Model .. Not appropriate for Thin-Film HJ Cells



Temperature dependence is completely wrong!

A new compact model for HJ Cells



$$J_{dark} = J_0 \left(\exp \left(\frac{qV}{NkT} \right) - 1 \right)$$

Silverman et al., JPV, 2015.

we solve the electron continuity equation **ONLY** considering the **generated** carriers

$$D \frac{\partial^2 n_{gen}(x)}{\partial x^2} + \mu E(x) \frac{\partial n_{gen}(x)}{\partial x} + G(x) = 0$$

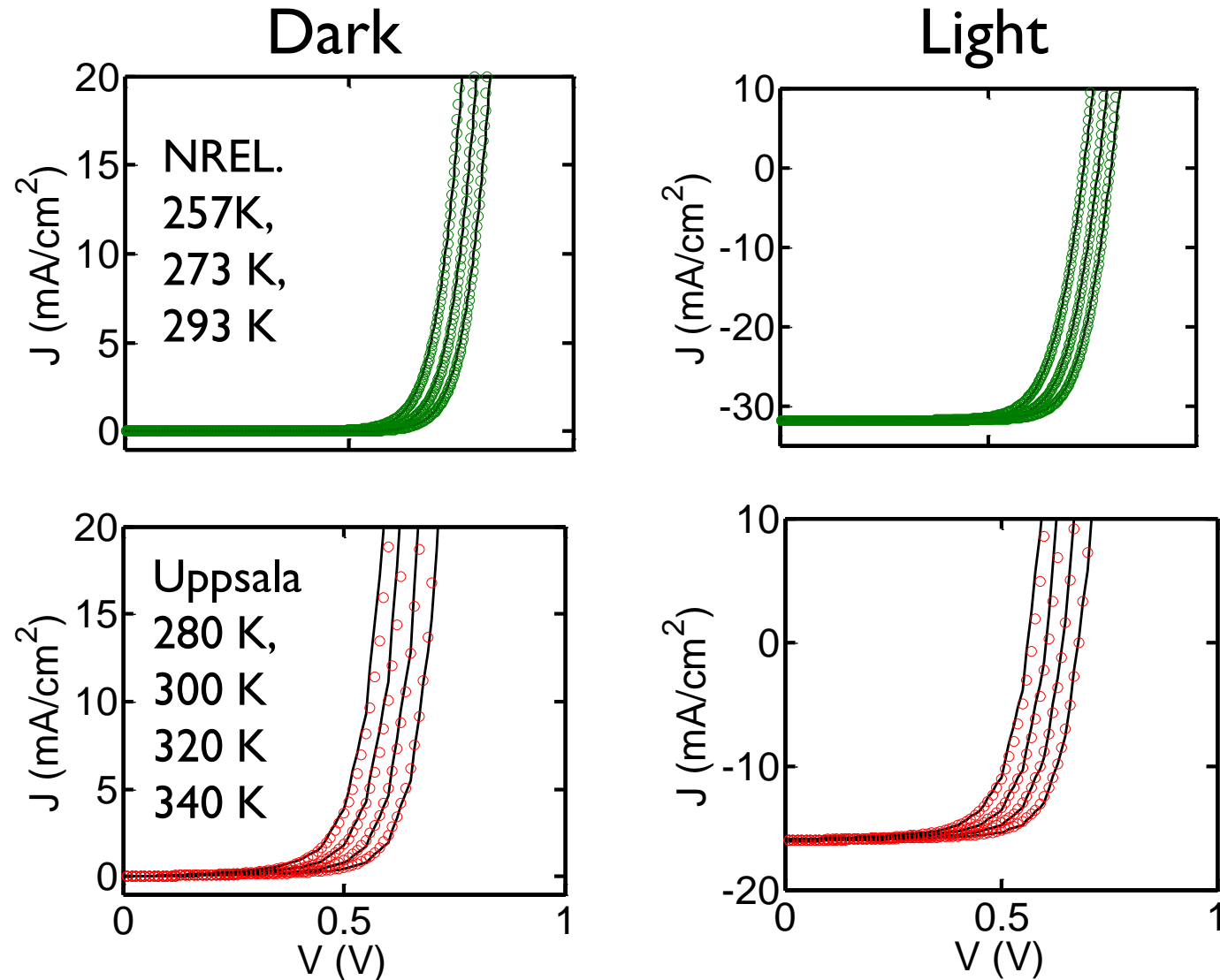
$$J_{photo,n} = q\mu E(x)n_{gen}(x) - qD \frac{\partial n_{gen}(x)}{\partial x}$$

$$J_{photo} = \frac{J_{tot} \left(1 - e^{-\chi \sqrt{\frac{V_{bi}-V}{V}}} \right)}{1 + \alpha_c e^{\beta \frac{q(V-V_{bi})}{kT}}}$$

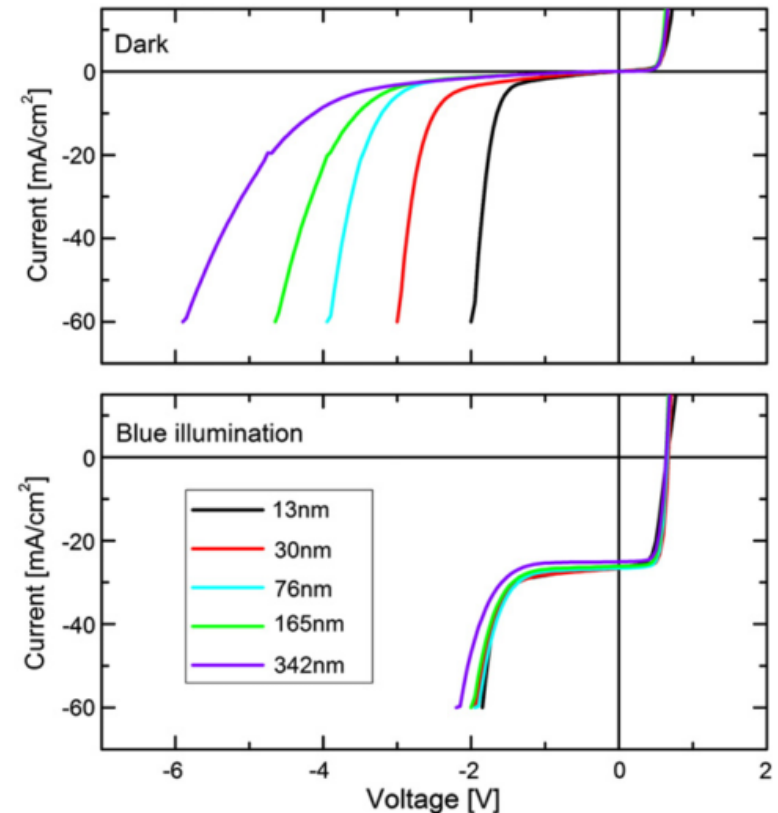
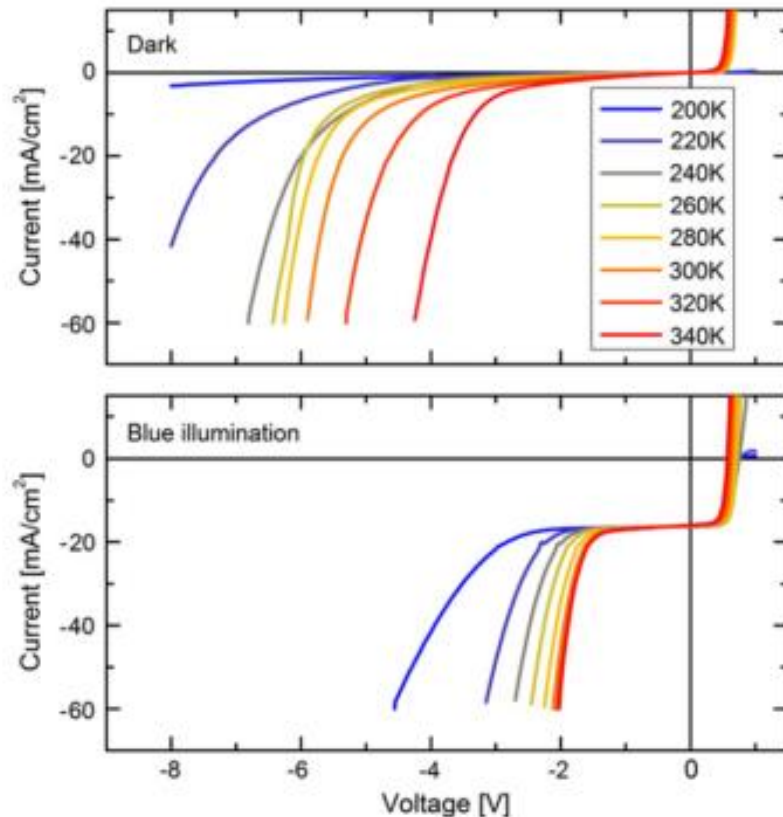
$$\chi = \frac{W_{delp}(0V)}{\lambda_{ave}}$$

$$\alpha_c = \frac{S_{n,b}}{S_{n,f}}$$

Model Captures CIGS Response

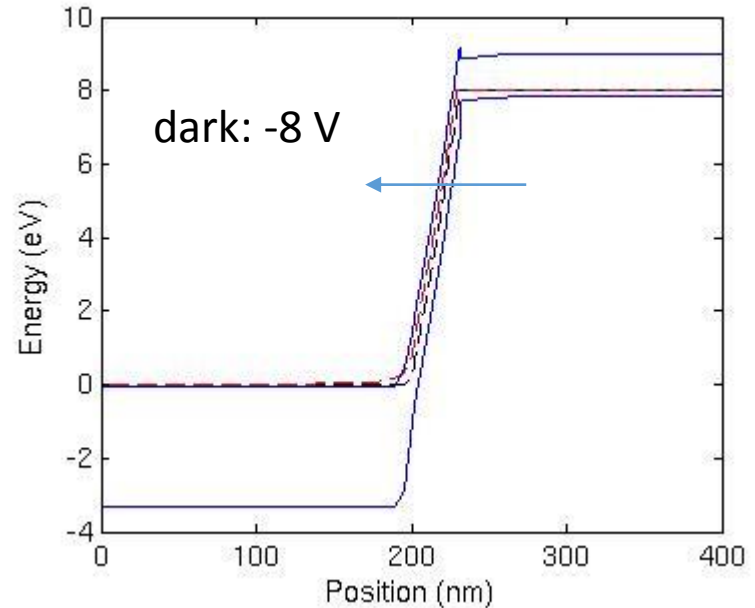
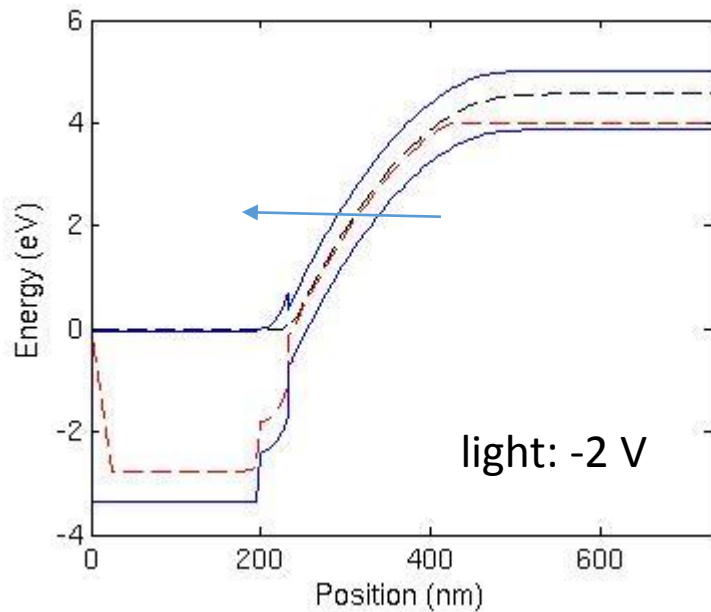


Model Captures Light Enhanced Breakdown



P. Szaniawski, J. Lindahl, T. Törndahl, U. Zimmermann, and M. Edoff,
“Light-enhanced reverse breakdown in Cu(In,Ga)Se₂ solar cells,” *Thin Solid Films*, vol. 535, pp. 326–330, May 2013.

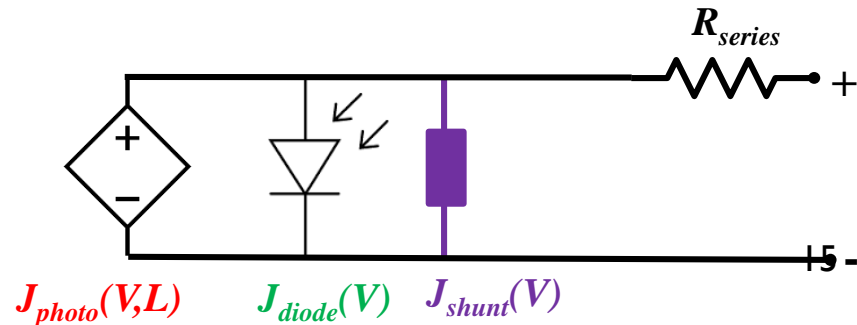
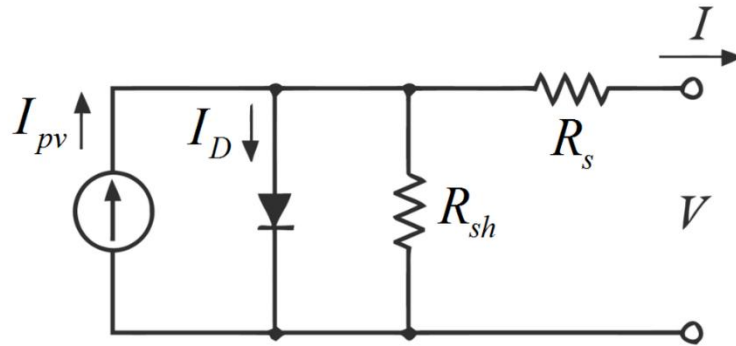
A very strange diode in Reverse Bias



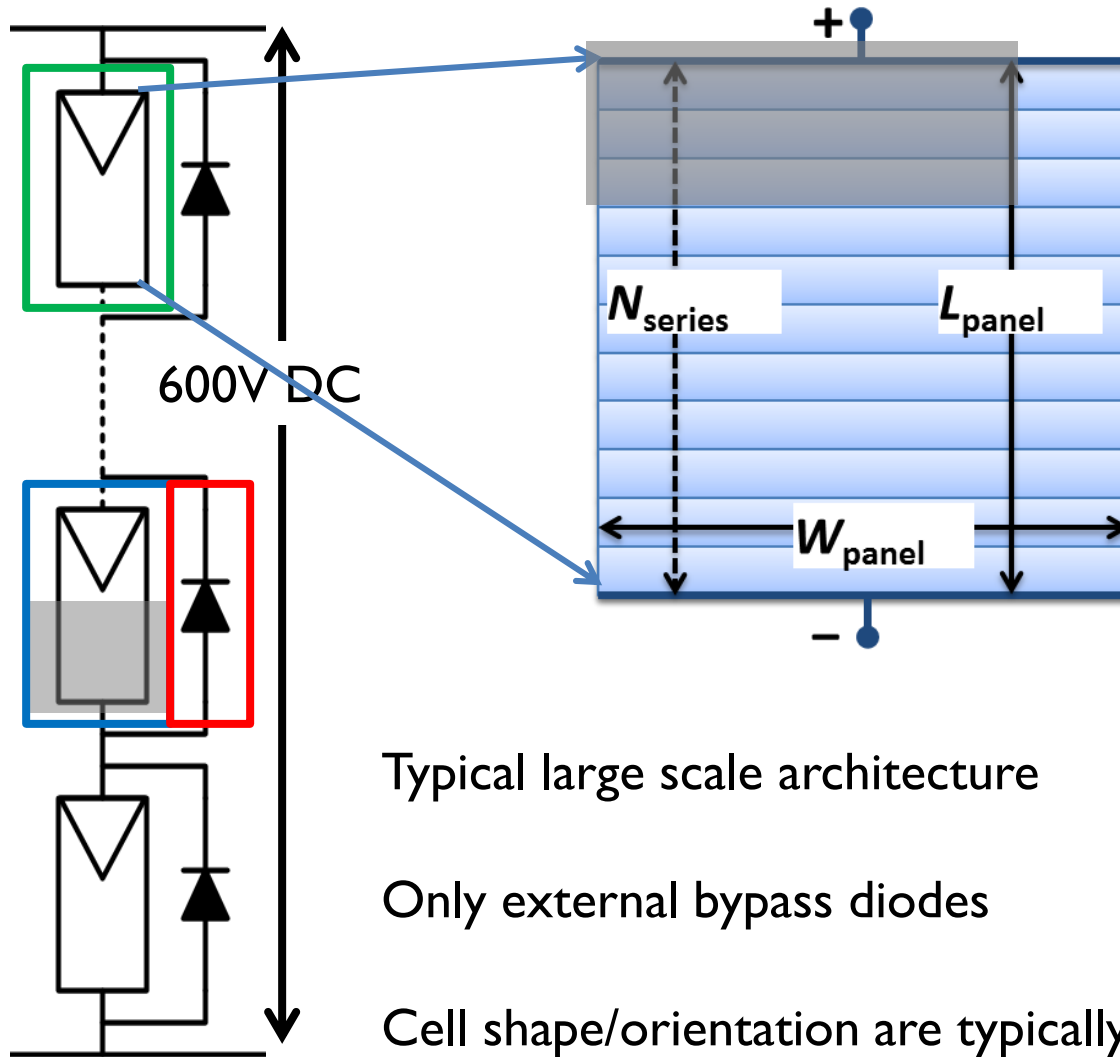
$$J_{FP} = J_0 \frac{V}{t} \exp \left(\frac{q}{kT} \sqrt{\frac{q}{\pi \epsilon_o \epsilon_{buffer}}} \sqrt{\frac{V}{t}} \right)$$

$$J_0 \sim \exp \left(-\frac{q \Phi_{defect}}{kT} \right)$$

New Compact Model



Partial shading in string architecture



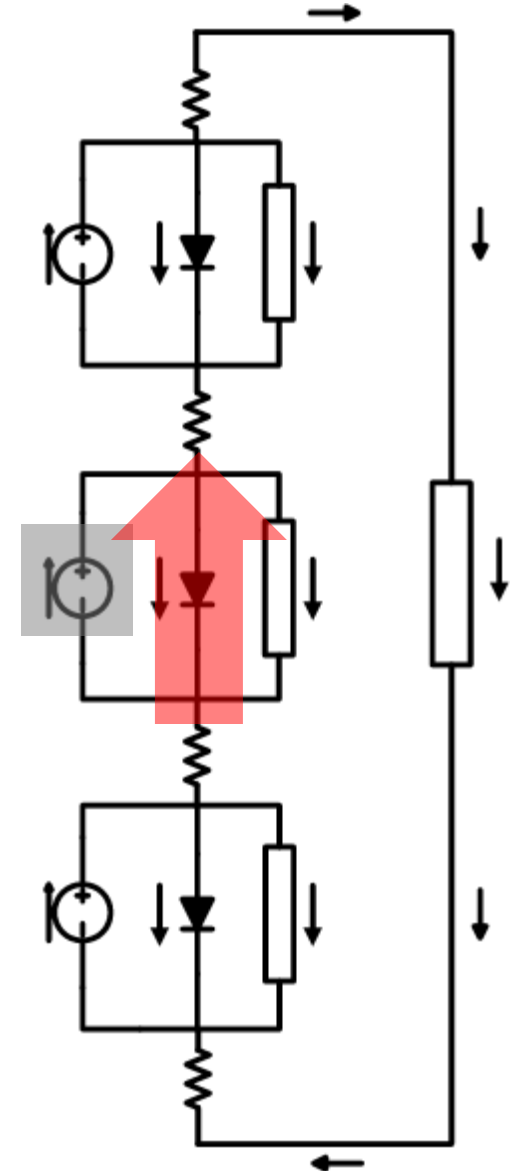
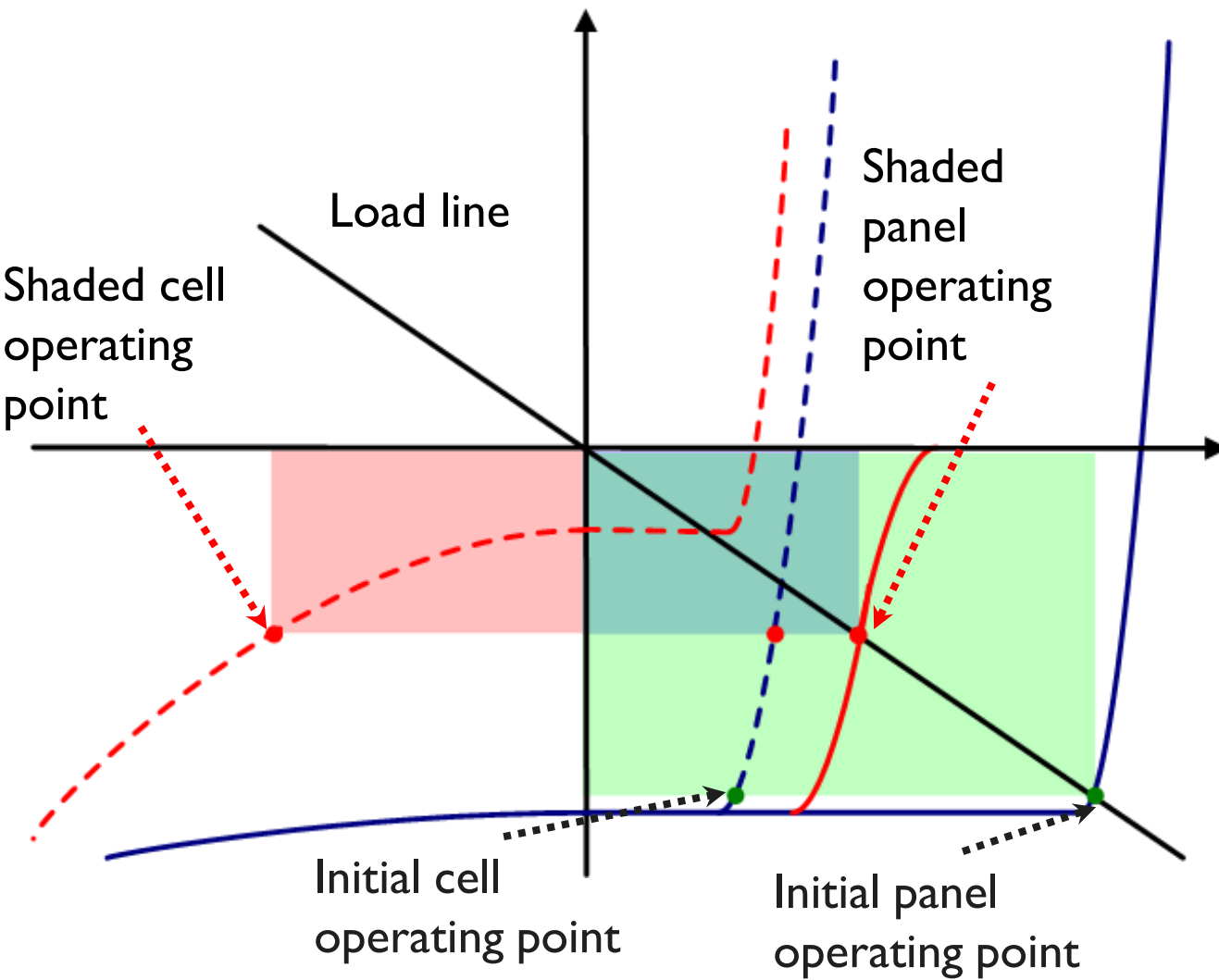
Typical large scale architecture

Only external bypass diodes

Cell shape/orientation are typically not considered



Being in shadow stresses the device



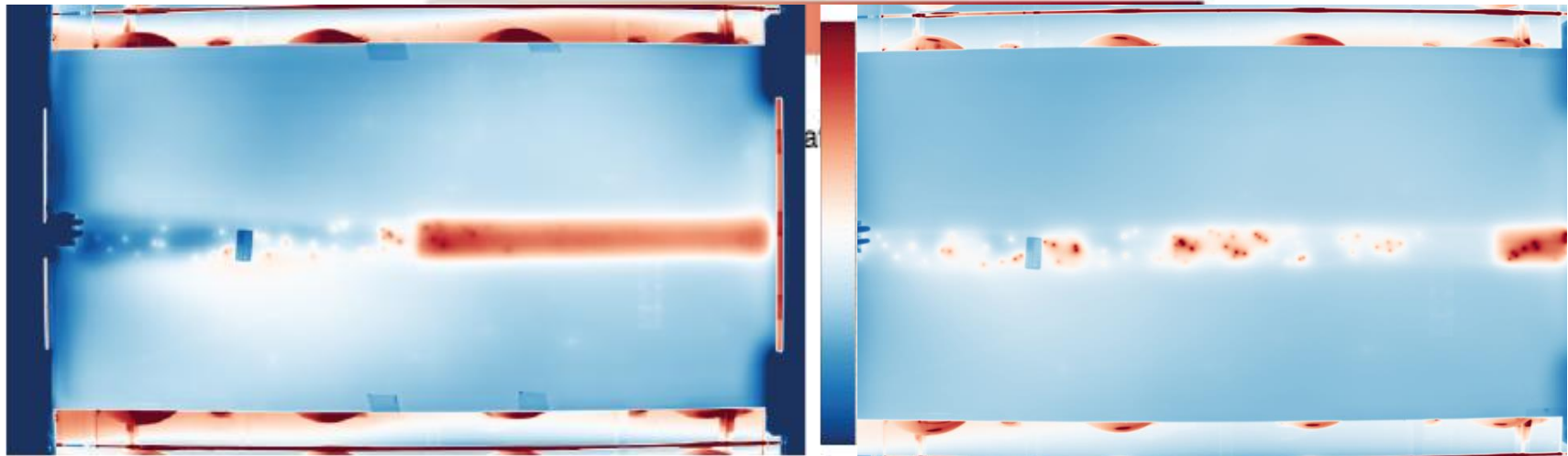
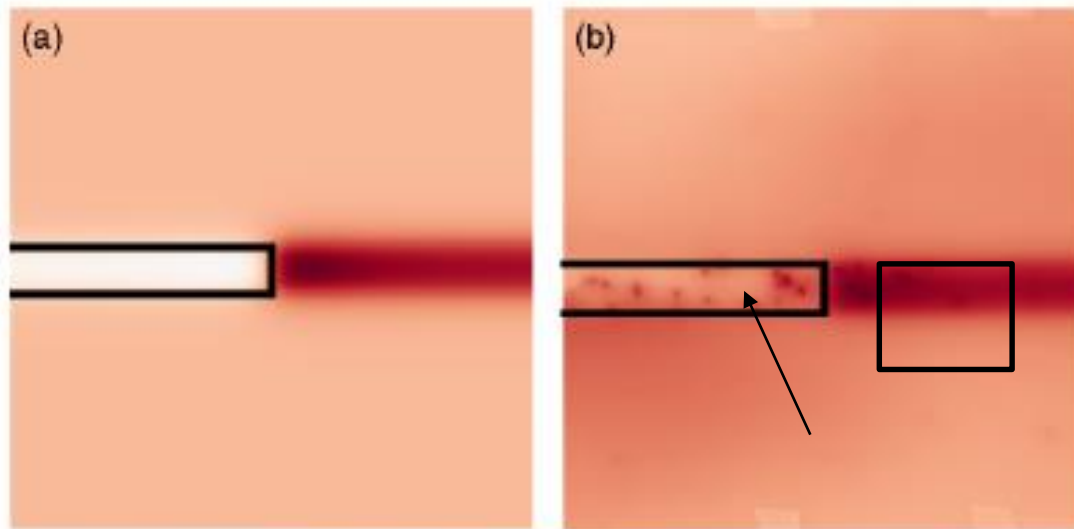
Shaded cells can get reverse biased!

© 2014 Apple Pumps and Systems, Inc.

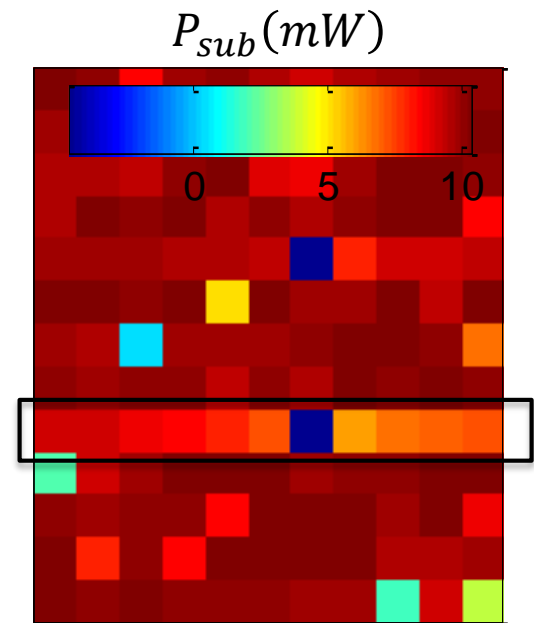
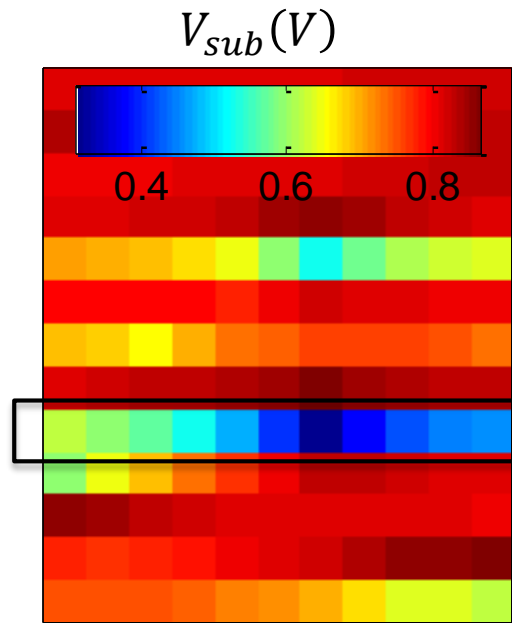
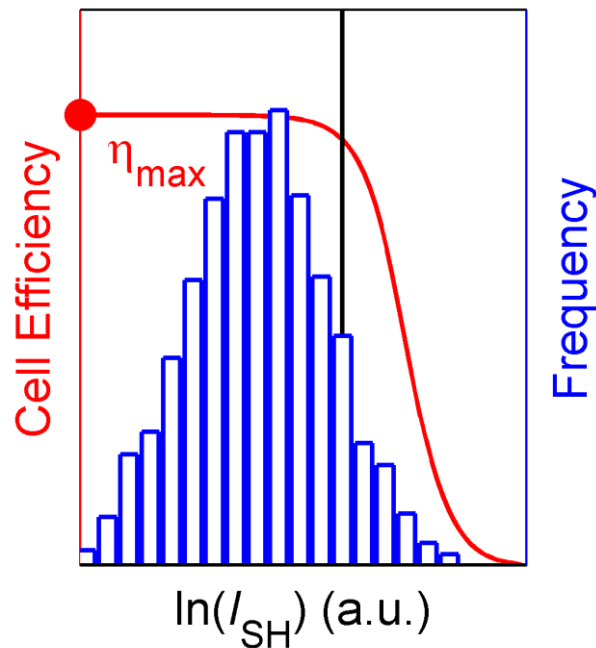
Simulation reproduces experiments

Simulation

IR image



Impact of heavy tailed shunt distribution



Heavy tail of shunt distribution determines the number of low efficiency shunted cells

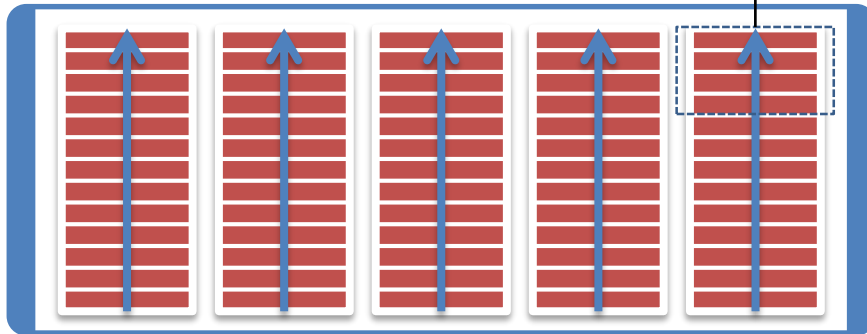
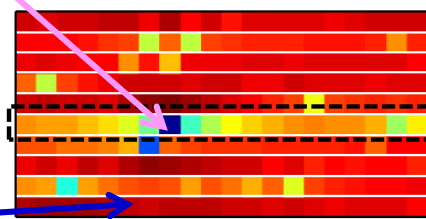
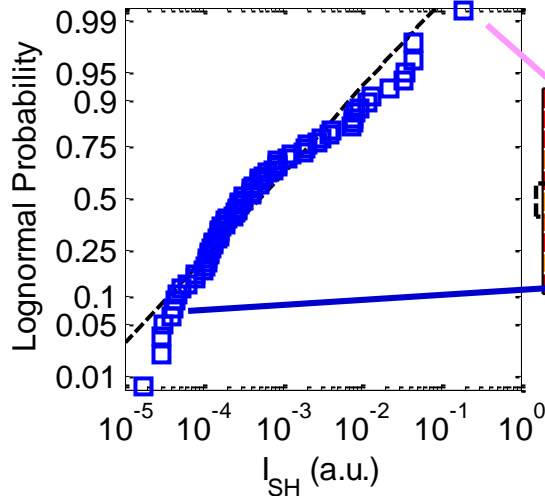
Shunted cells modify the bias of entire row, affecting the power output of their neighbors

Shunted cells drain the power output of neighbors, with disproportionate impact on module output

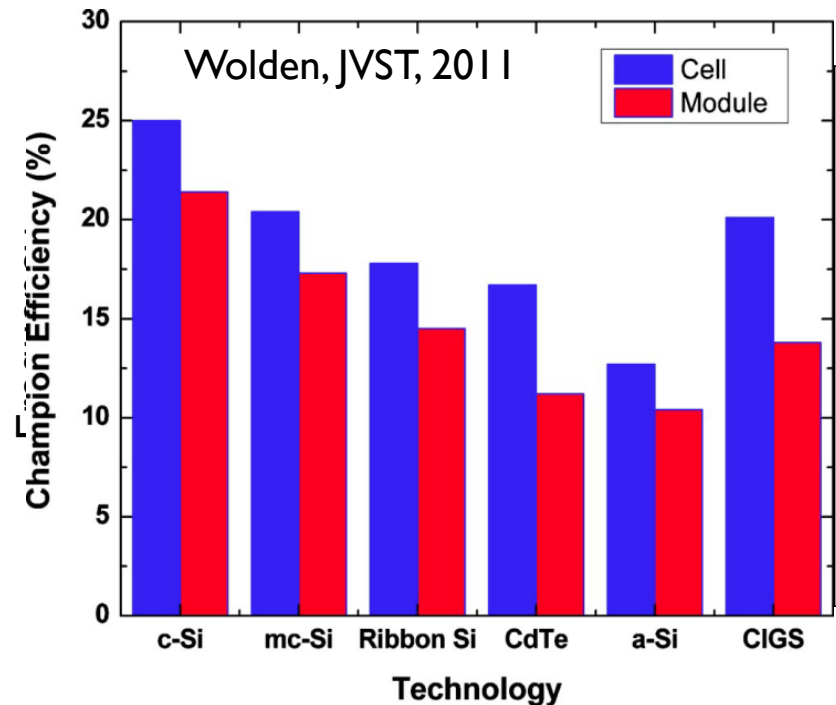
Long range interaction between sub-cells determines module performance loss

Panel vs. Cell Efficiency Gap Universal ?!

Shunts distributed
within module



shunt and series
resistance explain the gap

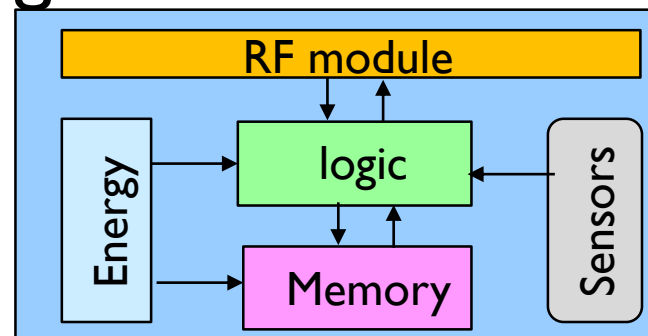


Cell/panel gap is essentially technology agnostic

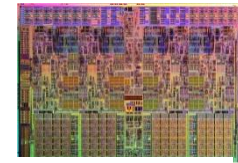
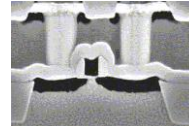
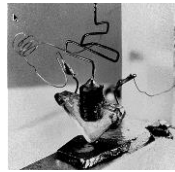
M. A. Green, Purdue University, 2015

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Back-story: A Century-long Convergence

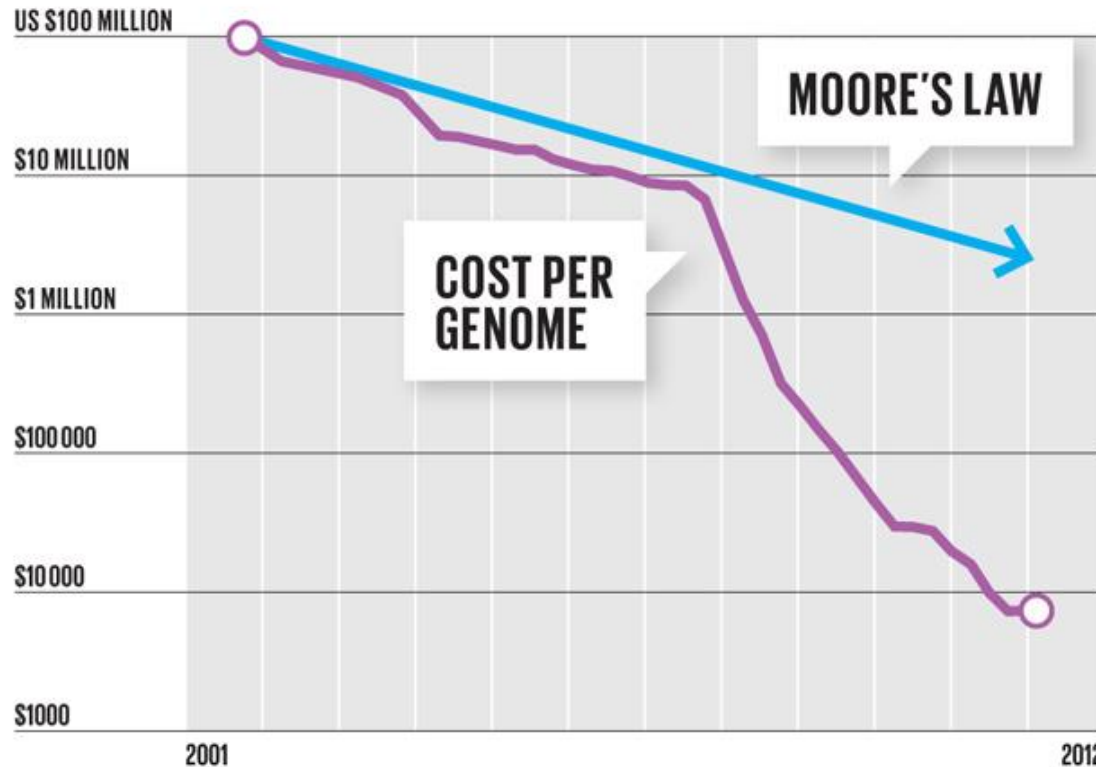


Vac. tube

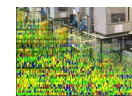
pH-meter



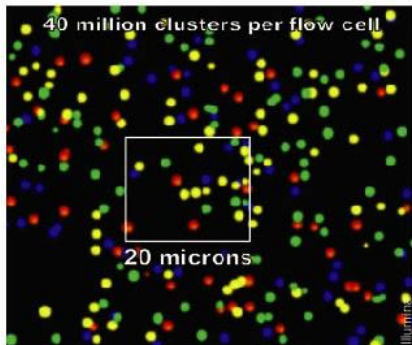
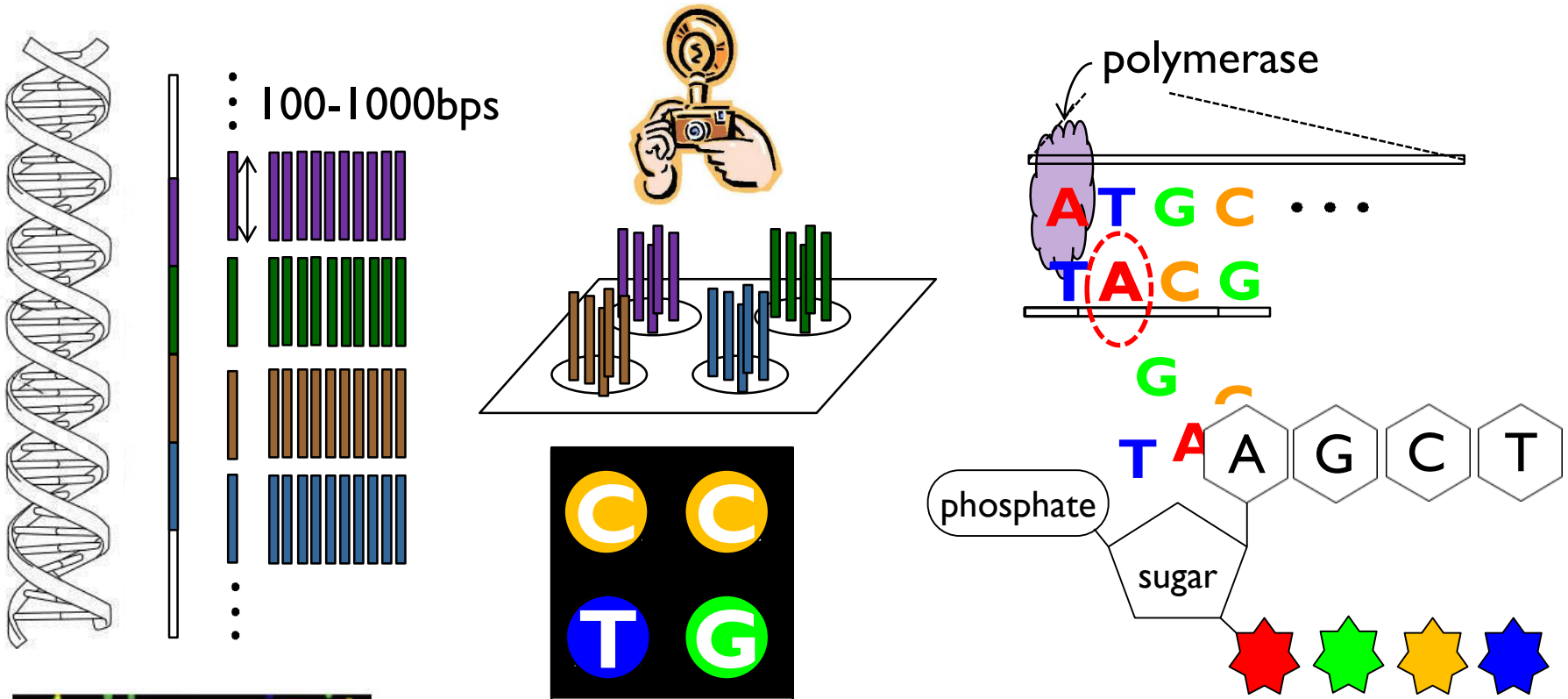
Virus/bacteria



Ion torrent



Conventional Sequence-by-Synthesis

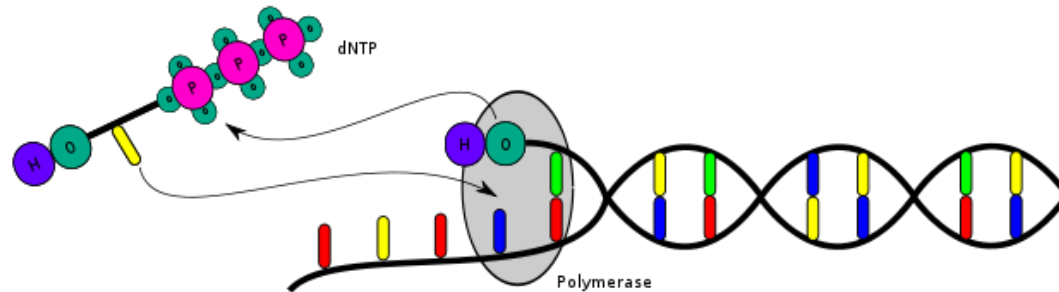


Courtesy of Illumina

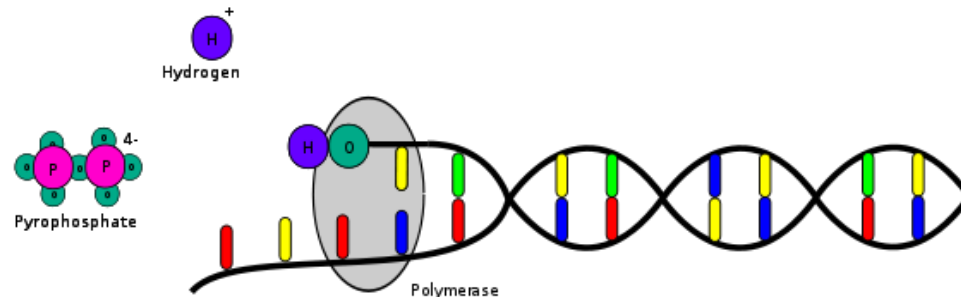
- Optical detection scheme expensive, because
- tagging of bases with fluorescent dye
 - bulky and expensive optical detector
 - processing costs of high volume images

DNA Synthesis releases Proton

deoxyribonucleotide
triphosphate (dNTP)



Polymerase integrates a nucleotide.



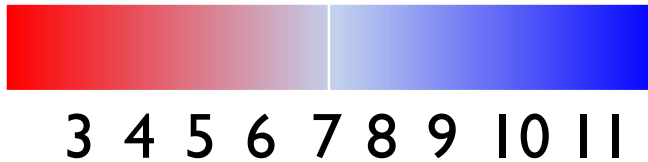
Hydrogen and pyrophosphate are released.



ISFET: Theory of pH-sensing

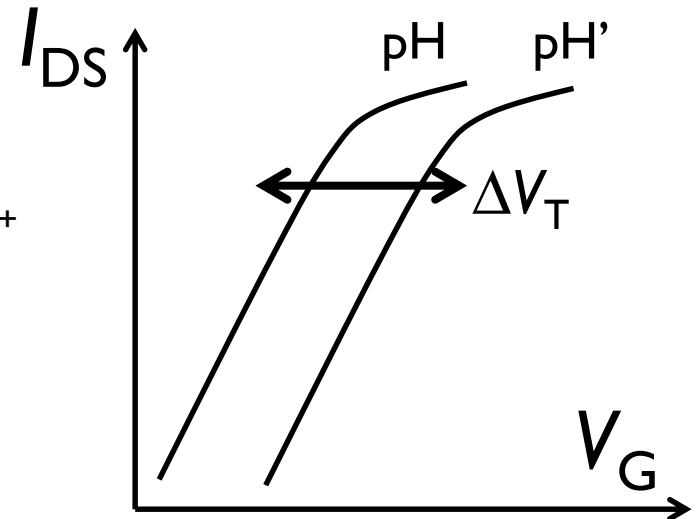
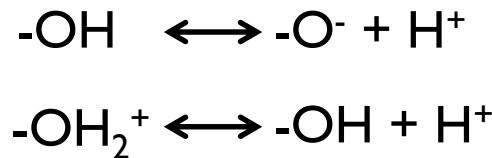
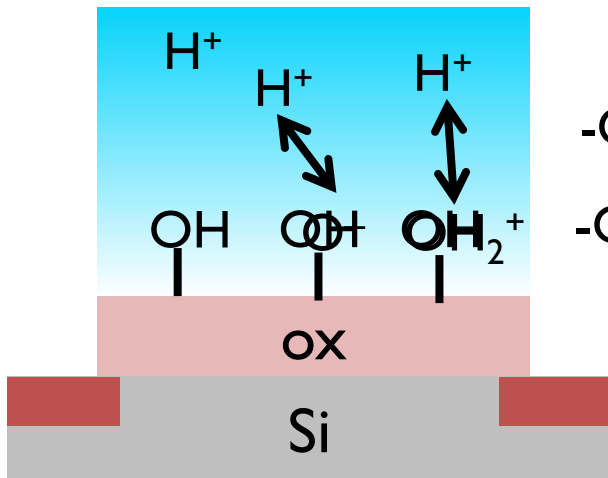
Acid

Alkaline



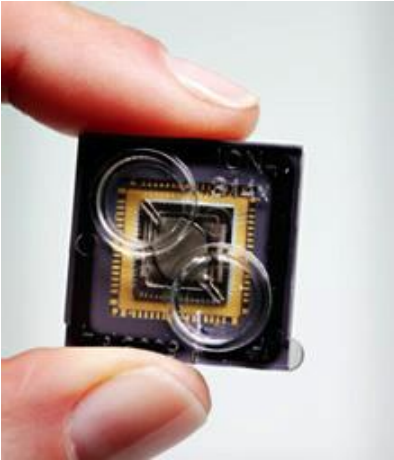
$$\text{pH} = -\log_{10} [\text{H}^+]_{\text{B}}$$

$$[\text{H}^+]_{\text{B}} = 10^{-7} \text{ M} \Rightarrow \text{pH} = 7$$

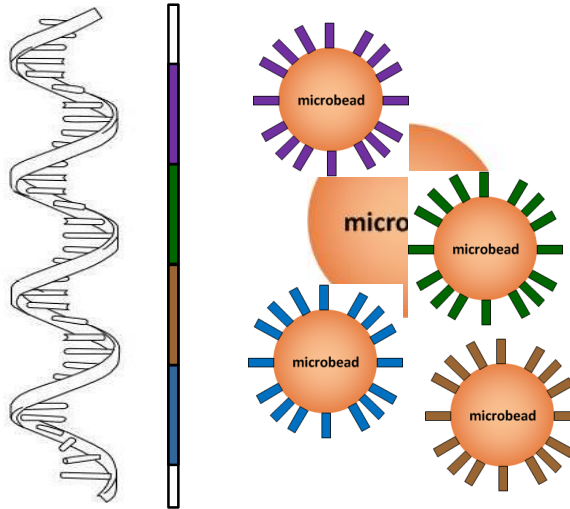


pH sensitivity $\equiv \Delta V_T / \Delta \text{pH} < 59 \text{ mV/pH}$ (Nernst limit)

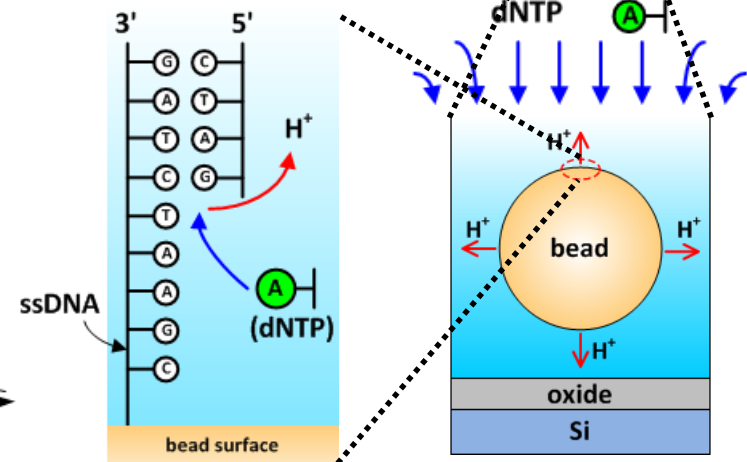
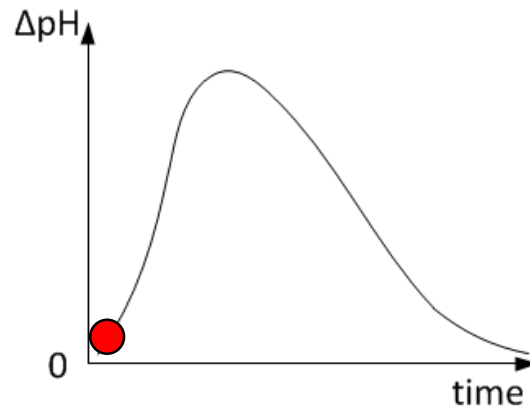
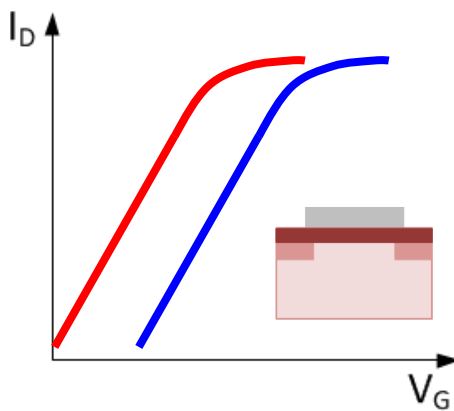
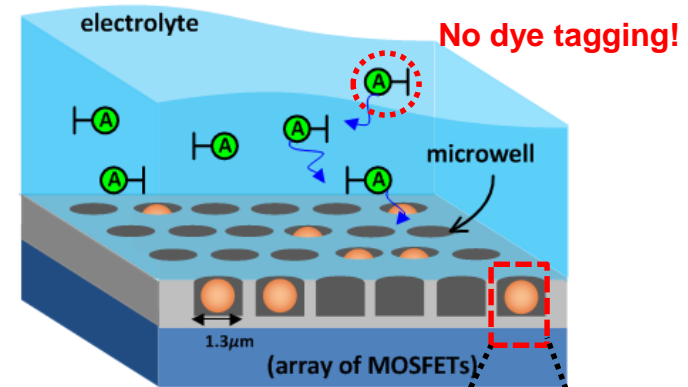
pH-based Genome Sequencers



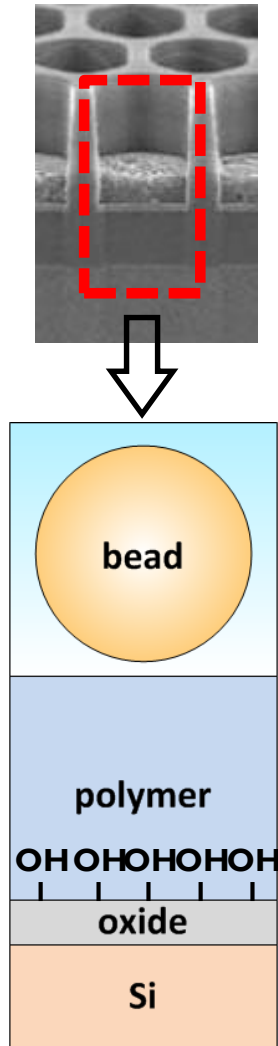
Courtesy of Ion Torrent



Reference: Rothberg et al., Nature 2011



Modeling Approaches (Go, JAP, 2013)



- Proton diffusion:

$$\frac{\partial(\Delta\rho_H)}{\partial t} = D_H \nabla^2(\Delta\rho_H)$$

- ISFET electrostatics

$$-\nabla \cdot (\epsilon \nabla \Psi) = \rho$$

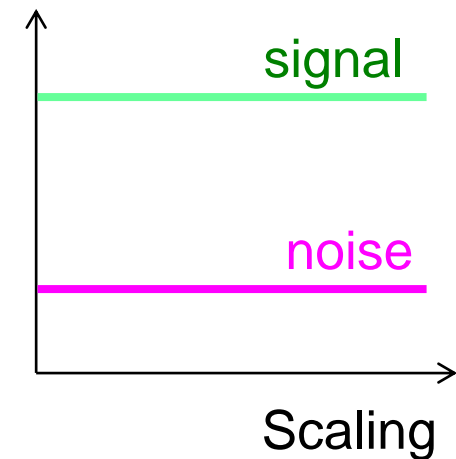
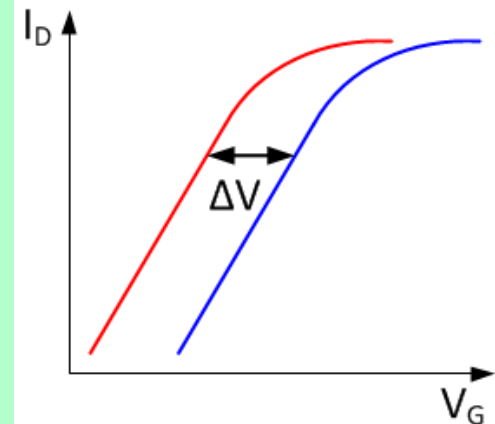
- Reaction of OH groups¹

$$\sigma_{OH} = qN_s \frac{10^{pK_a - pH_S} - 10^{pH_S - pK_b}}{1 + 10^{pK_a - pH_S} + 10^{pH_S - pK_b}}$$

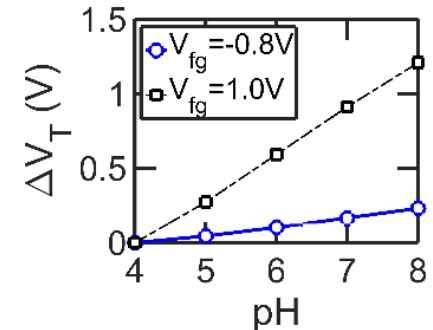
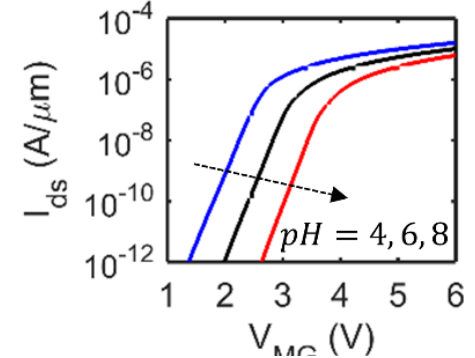
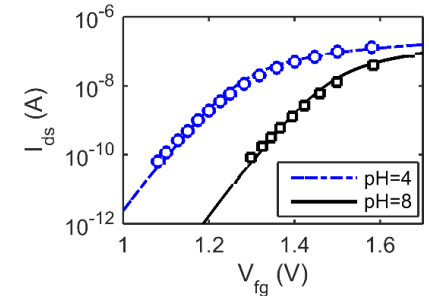
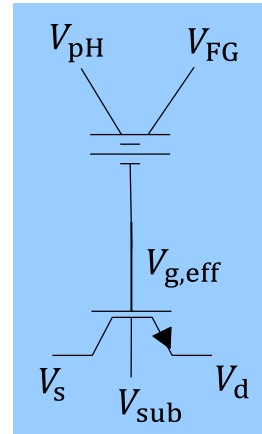
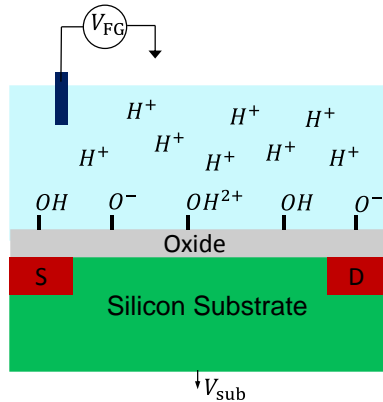
¹Landheer et al., JAP 2005

- 1/f noise of ISFET²

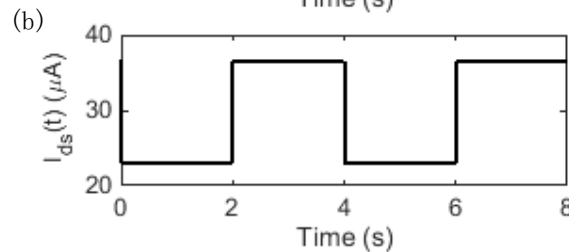
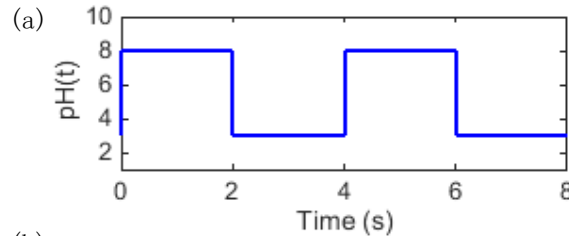
$$\delta V_G = \sqrt{\frac{q^2 k_B T N_t \lambda}{W L C_{eff}^2}} \left[1 + \left(\alpha \mu_{eff} C_{eff} \frac{I_{DS}}{g_m} \right) \right] \log \left(\frac{f_2}{f_1} \right)$$



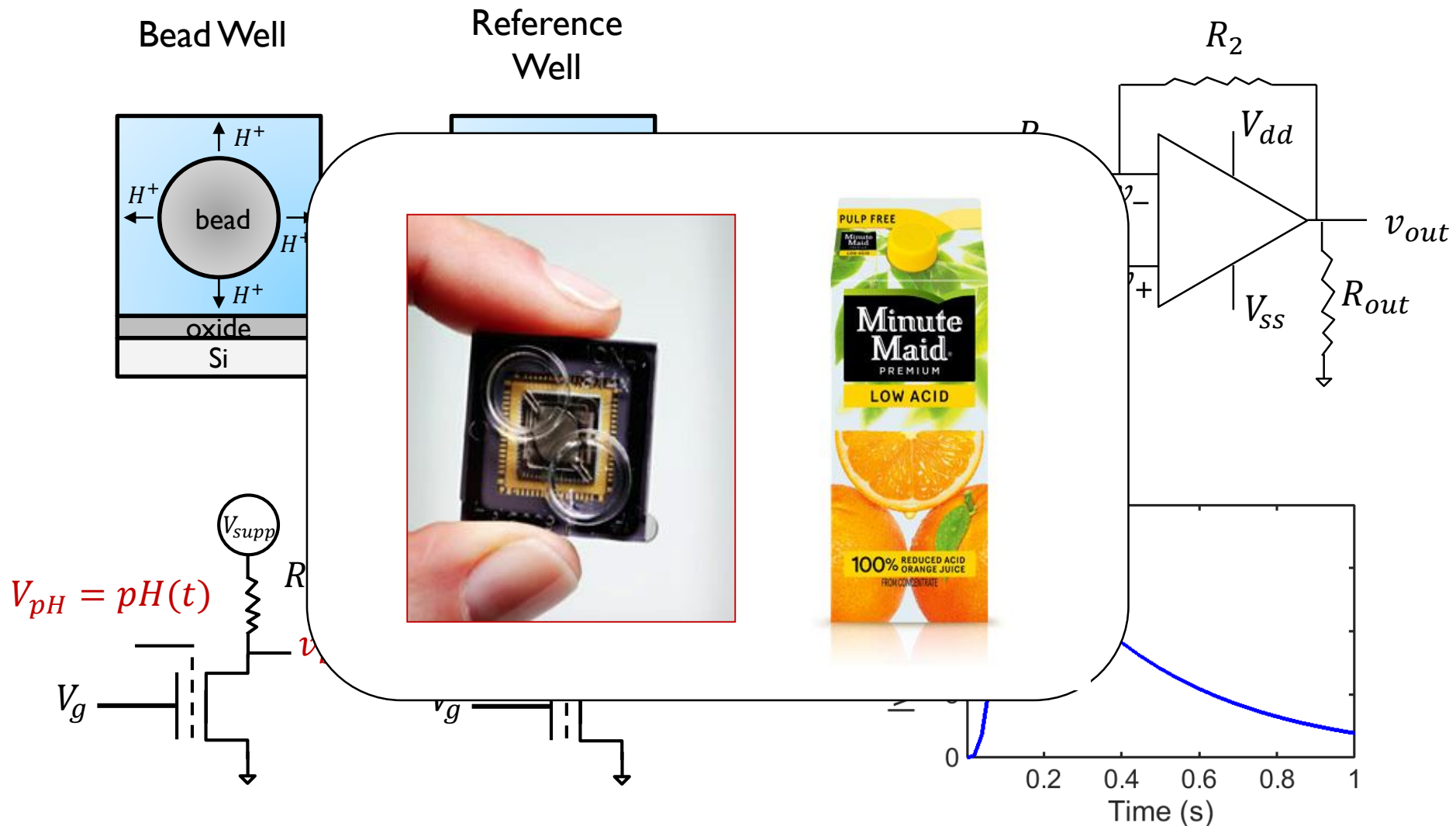
A Physics-based Compact Model



$\sigma_{dl} + \sigma_{OH} + \sigma_{mos} = 0$	(1)
$AOH_2^+ \rightleftharpoons AOH + H_s^+$	K_a (2)
$AOH \rightleftharpoons AO^- + H_s^+$	K_b (3)
$\sigma_{OH} = q([AOH_2^+] - [AO^-])$ $= -2qN_s \frac{(\tanh(q\psi_e/kT + 2.3 \Delta pH))}{(10^{\Delta pK/2} \text{sech}(q\psi_e/kT + 2.3 \Delta pH))}$	(4)
$\psi_e = \psi_0 + \sigma_{OH}/C_{stern}$	(5)
$\sigma_{dl} = -\sqrt{8kT\epsilon_w n_0} \sinh\left(\frac{q\psi_0}{2kT}\right)$	(6)
$\psi_e = \frac{2kT}{q} \text{asinh}\left(\frac{\sigma_{OH}}{\sqrt{8kT\epsilon_w n_0}}\right) + \frac{\sigma_{OH}}{C_{stern}}$	(7)
$V_{g,eff} = V_{fg} + \psi_e$	(8)
$\Delta pH = pH - (pK_a + pK_b)/2$	(9)
$\Delta pK = pK_b - pK_a$	
$pK_a = -\log_{10}(K_a), pK_b = -\log_{10}(K_b)$	(10)

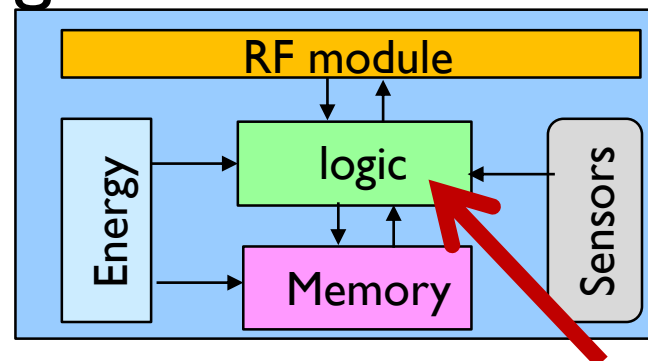


Differential Amplifier Circuit Used

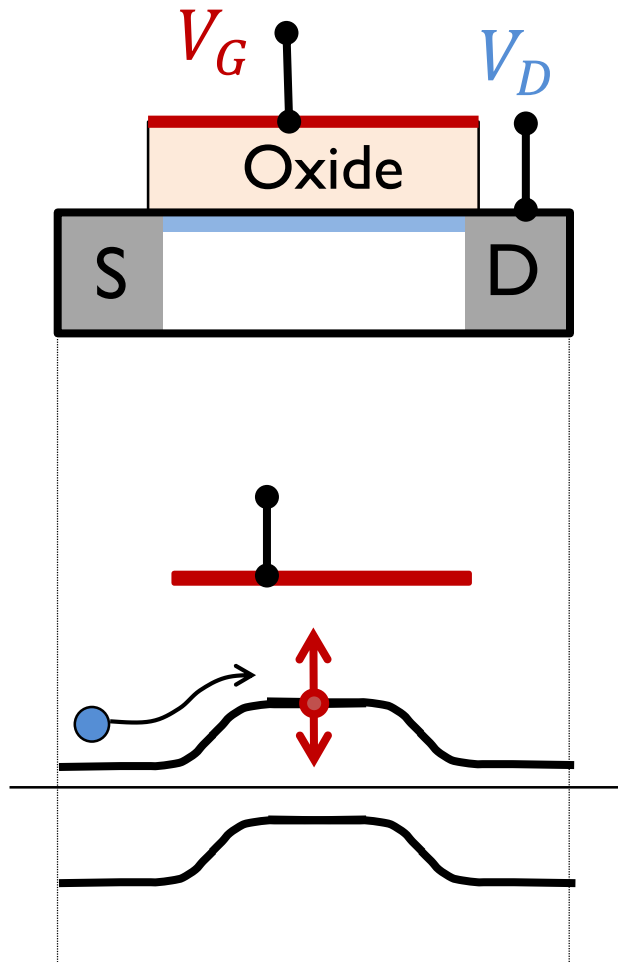


Outline

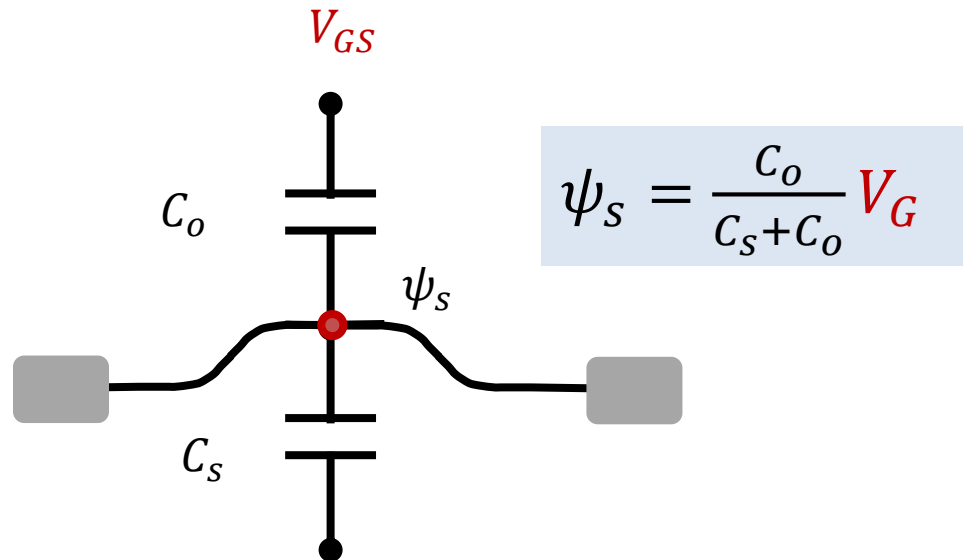
- Is there a life after Moore's Law
- Power sources: Harvesters, solar cells, etc.
- Implantable and clinical nanobiosensors
- Low-power Landau switches
- The challenges of integrated simulation
- Conclusions



Capacitors control MOSFET Operation

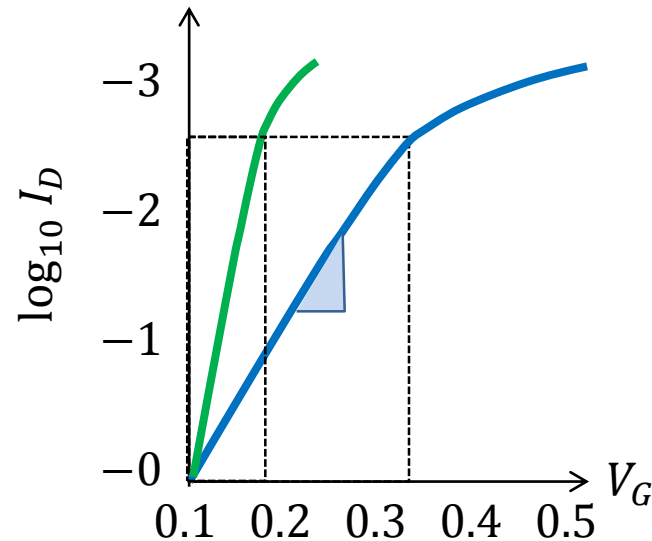
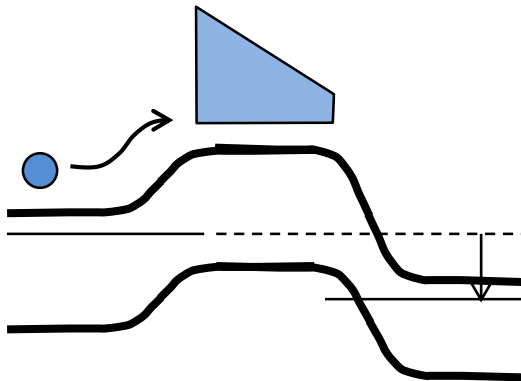


$$m = \frac{dV_G}{d\psi_s} = 1 + \frac{C_s}{C_o}$$



Subthreshold Slope describes Transistors Performance

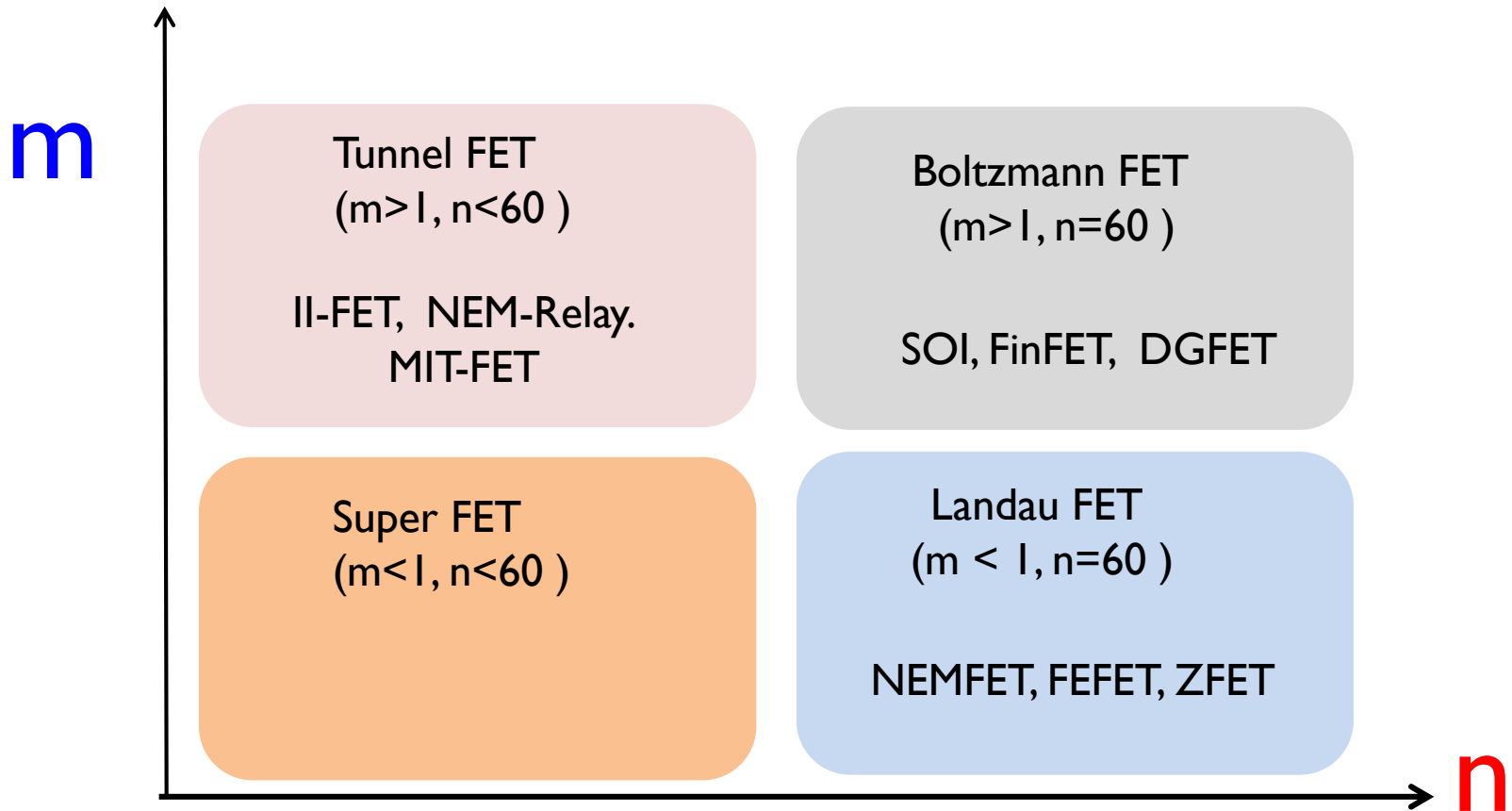
$$I_D = I_0 e^{\frac{q\psi_s}{kT}} \left(1 - e^{-\frac{qV_D}{kT}}\right) \sim I_0 e^{\frac{q\psi_s}{kT}} = I_0 e^{qV_G/mkT}$$



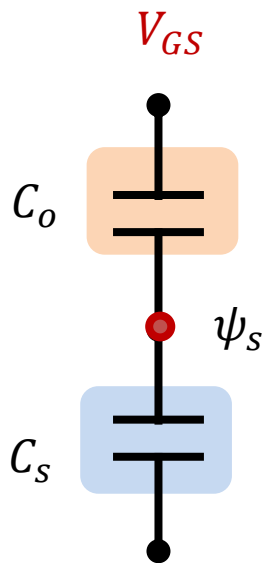
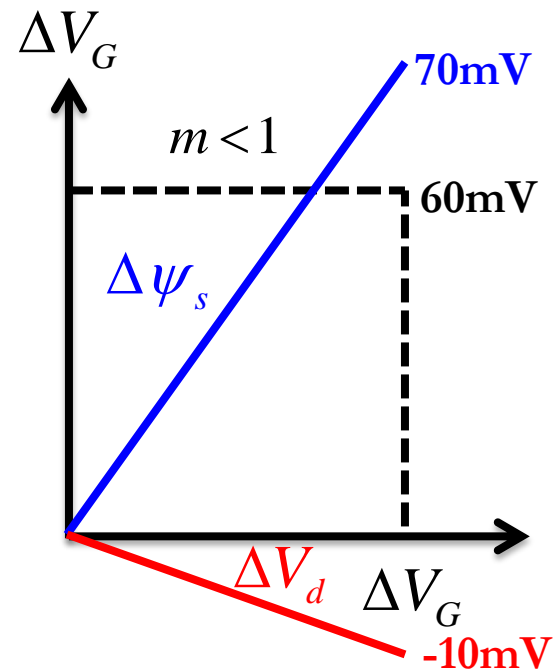
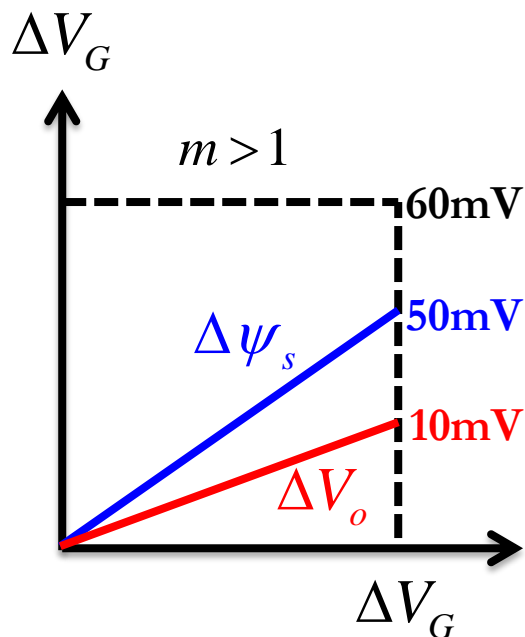
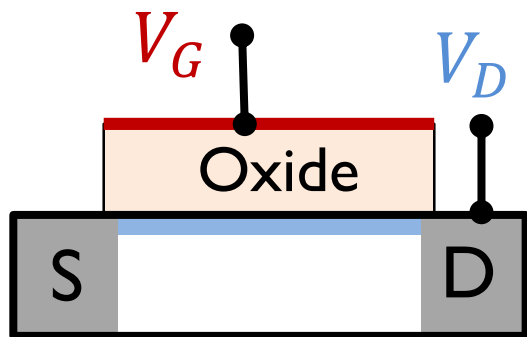
$$S \equiv \left[\frac{d \log_{10}(I_{DS})}{dV_G} \right]^{-1} = \left[\left(\frac{d\psi_s}{dV_G} \right) \left(\frac{d \log_{10}(I_{DS})}{d\psi_s} \right) \right]^{-1} = m \times n = m \times 60 \text{ mV/dec}$$

Phase Space of FET

$$S \equiv \left[\left(\frac{d\psi_s}{dV_G} \right) \left(\frac{d \log_{10} (I_{DS})}{d\psi_s} \right) \right]^{-1} = m \times n$$



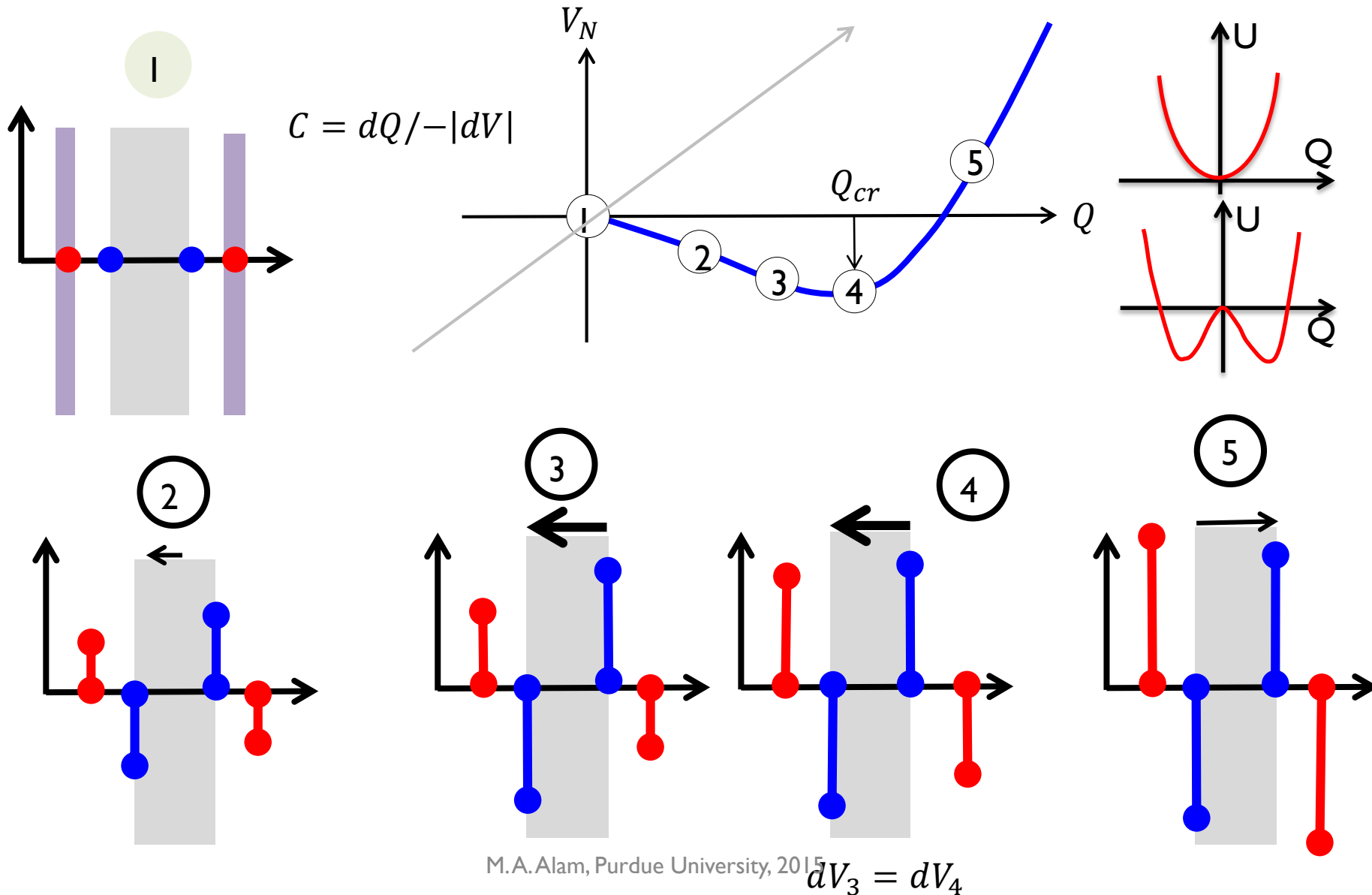
$S < 60 \text{ mV/dec}$ switching?



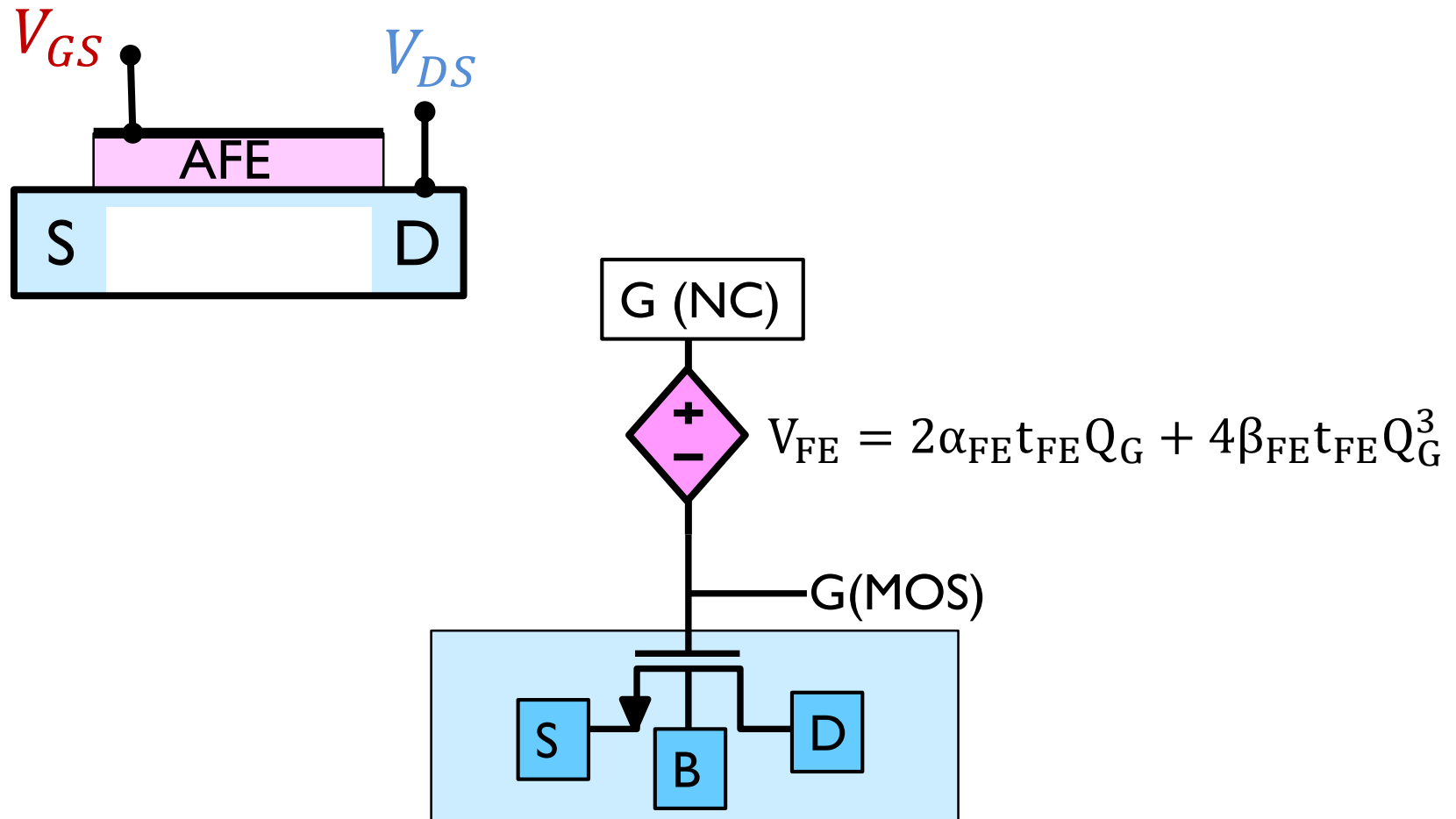
$$S = m \times 60 \text{ mV/dec}$$

$$m = \frac{dV_G}{d\psi_s} = 1 + \frac{C_s}{C_o}$$

Single ferroelectric charge profile



Coupling of Capacitors: Algorithm



MVS-compact model

$$I_D/W = Q_{ix_o} v_{x_o} F_s$$

$$F_s = \frac{V'_{DS}/V_{DSAT}}{\left(1 + (V'_{DS}/V_{DSAT})^\beta\right)^{1/\beta}}$$

$\beta \rightarrow$ saturation-transition-fitting parameter

$$Q_{ix_o} = C_{inv} n \phi_t \ln \left(1 + \exp \frac{V'_{GS} - (V_T - \alpha \phi_t F_f)}{n \phi_t} \right)$$

$n \rightarrow$ sub-threshold coefficient
 $\alpha \rightarrow$ fitting parameter

$$V_T = V_{T0} - \delta V'_{DS} \quad \delta \rightarrow \text{DIBL coefficient}$$

$$V_{DSAT} = V_{DSATs}(1 - F_f) + \phi_t F_f$$

$$V_{DSATs} = \frac{v_{x_o} L_C}{\mu}$$

$v_{x_o} \rightarrow$ sort of saturation velocity
 $\mu \rightarrow$ sort of low field mobility

$$F_f = \frac{1}{1 + \exp \left(\frac{V'_{GS} - (V_T - \alpha \phi_t / 2)}{\alpha \phi_t} \right)}$$

$F_f \rightarrow$ Fermi function for smooth transition

$$\gamma = \sqrt{2q\epsilon_{Si}\bar{N}}/C_g$$

$\gamma \rightarrow$ body factor

$$V'_{DS} = V_{DS} - I_D(R_S + R_D)$$

Voltage drop in R_S and R_D

$$I_D = I_D + I_D(V_{GS} = 0)$$

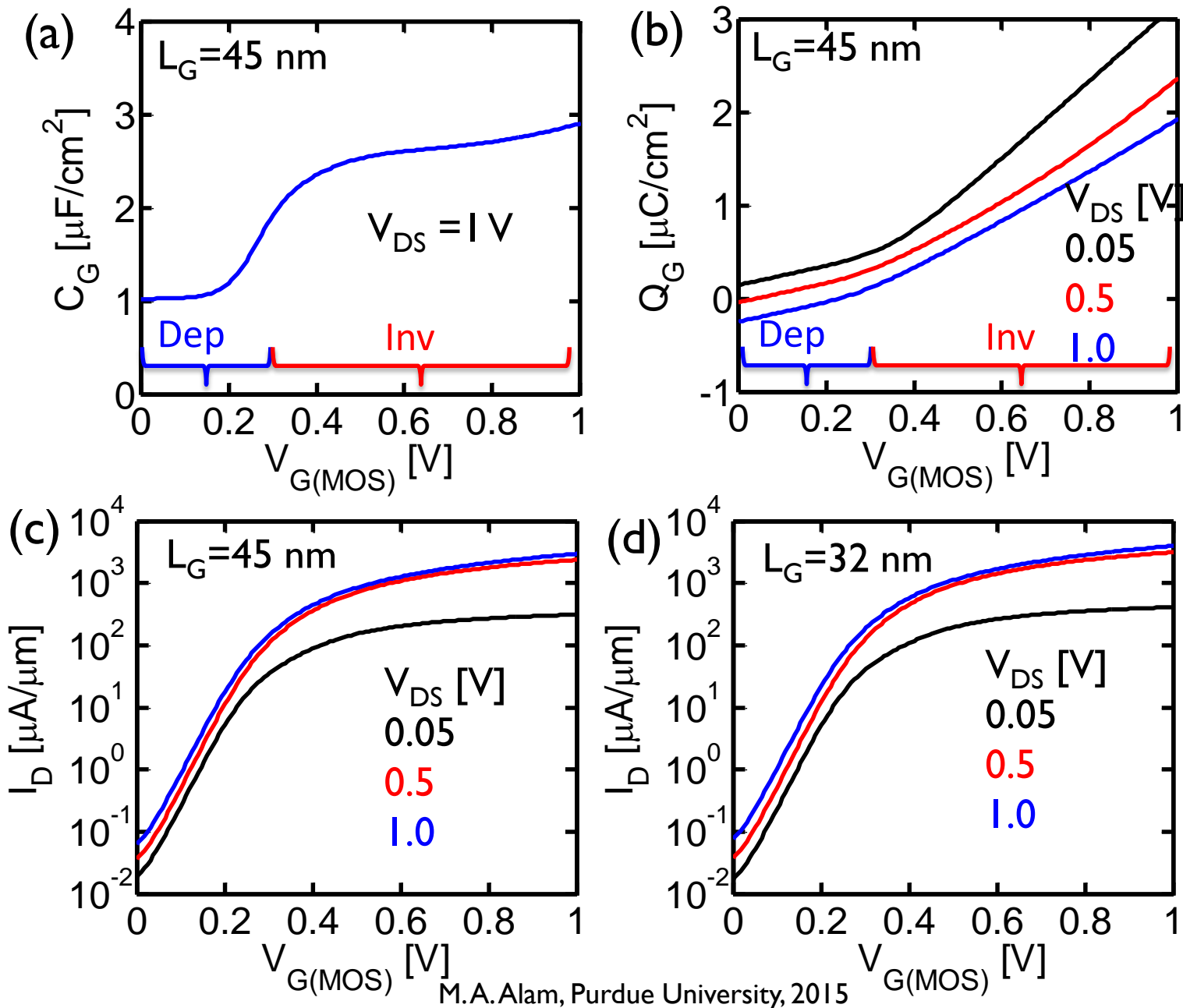
Current saturation in depletion/accumulation edge
 M. A. Alam, Purdue University, 2015

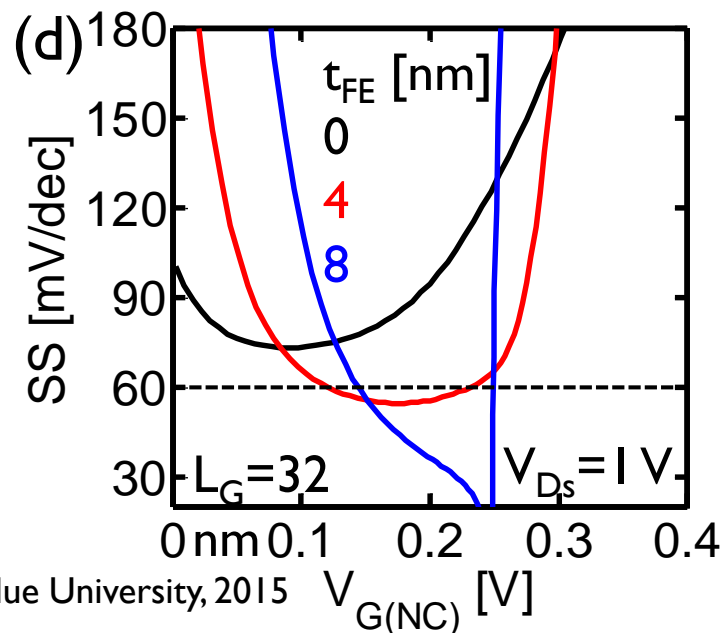
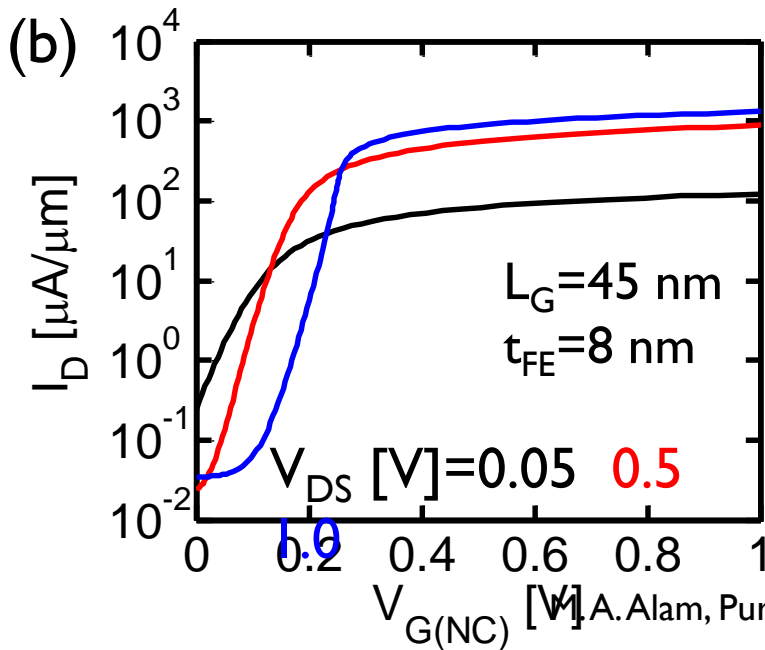
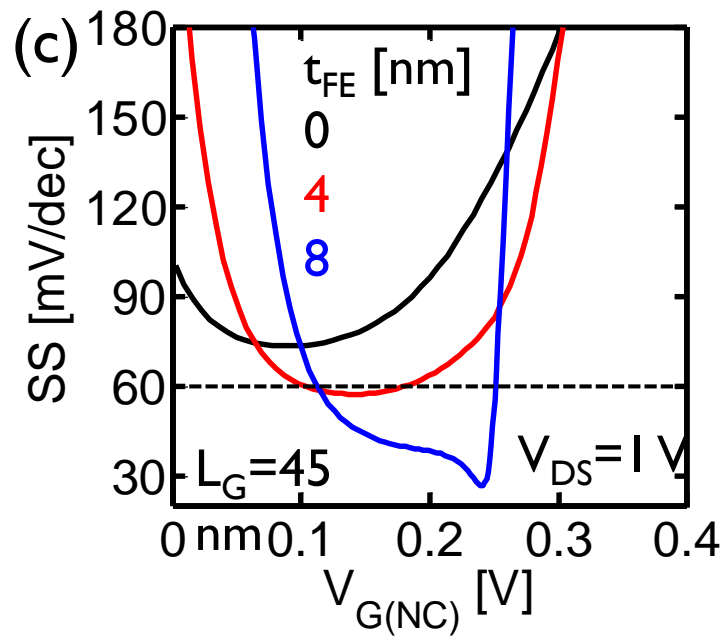
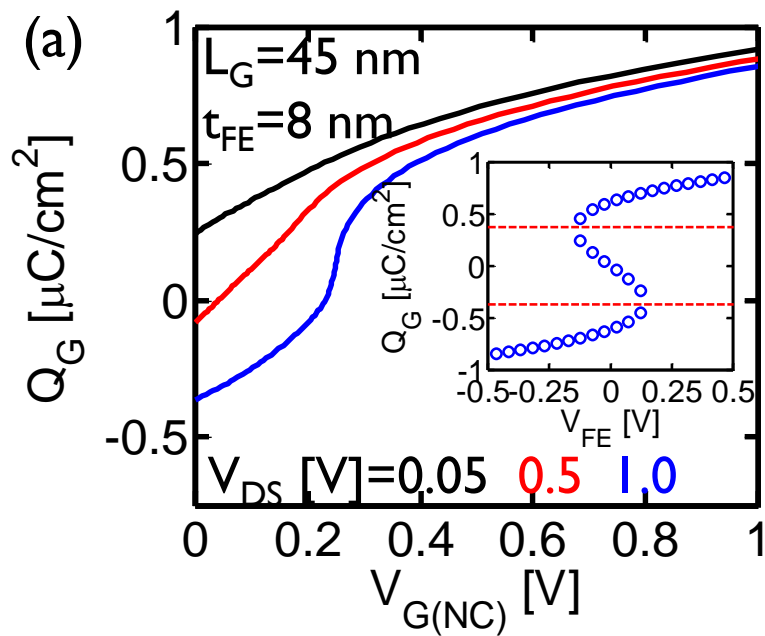
Khakifirooz, *TED*, 56 (2009) 1674

Wei, *TED*, 59 (2012): 1263

Rakheja, nanoHUB.

[doi:10.4231/D3HI2V82S](https://doi.org/10.4231/D3HI2V82S)





Conclusions

- There is (different) life after Moore's law.
- Power sources: Significant progress in terms of physics-based compact modeling of energy harvesters (e.g. solar cells).
- Biosensors can be transformative. Physics-based modeling is already playing a role in sequencing.
- Landau switches may obviate sub-threshold logic.

Acknowledgement: NEEDS

Goal: To advance the science of nano-devices and enable new applications.

Focus:

- 1) Physics-based compact models for emerging devices
- 2) Infrastructure to support the NEEDS team and the broader community.



Specific Infrastructure Objectives

- 1) Develop a suite of open-source, **physics-based** compact models for emerging nanodevices.
- 2) Develop **tools and processes** for creating, testing, and publishing “simulation-ready” compact models.
- 3) Develop **educational resources** to help beginners develop compact models and to convey the physical principles of new nano-devices.
- 4) Leverage **nanoHUB.org** to to engage a broad community of materials and device researchers and circuit and system designers.



NEEDS

NANO-ENGINEERED ELECTRONIC
DEVICE SIMULATION NODE

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Nano-Engineered Electronic Device Simulation Node

NEEDS has a vision for a new era of electronics that couples the power of billion-transistor CMOS technology with the new capabilities of emerging nano-devices and a charter to create high-quality models and a complete development environment that enables a community of compact model developers.

NEEDS Team: Purdue, MIT, U.C. Berkeley, and Stanford.

[REGISTER NOW](#) for the May 11-12 NEEDS annual meeting and workshop.

NEWEST COMPACT MODEL RELEASE: UCSB 2D Transition-Metal-Dichalcogenide (TMD) FET model 1.0.0. [See Compact Models Page](#)

NEEDS announces the public release of [Berkeley MAPP](#), a MATLAB-based platform for prototyping compact models and simulation algorithms.

GET STARTED ON COMPACT MODELING: Take Colin McAndrew's [online workshop](#).



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Physically-detailed simulations
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MODEL AND ALGORITHM PROTOTYPING PLATFORM (MAPP)

A Matlab-based platform for
prototyping models and
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FOR DEVELOPERS

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models and for creating compact
models with NEEDS tools and
processes



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